

1 **Dielectric properties of milk during ultra-heat treatment**

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16 **Abstract**

17 Dielectric properties are important for predicting dielectric heating of foodstuffs. The
18 dielectric properties of three types of milk (raw, skimmed and concentrated non-fat)
19 were analyzed at high frequencies between 10 MHz to 2450 MHz for producing
20 temperatures between 20 °C and 150 °C. The study of cow milk dielectric constants (ϵ'
21 and ϵ'') at conditions above 100 °C is needed to evaluate dielectric sterilization of milk.
22 The dielectric constant (ϵ') was found to decrease with frequency at all temperatures but
23 increase with temperature at low frequencies and decrease with temperature at high
24 frequencies. The dielectric loss factor (ϵ'') decreased with frequency and increased with
25 temperature in almost the entire range of frequencies. Ionic conduction was the
26 dominant mechanism across most of the frequency range. For milk samples with higher
27 ash content (related to salt content), ϵ' was higher at low frequencies and lower at high
28 frequencies, whereas ϵ'' was higher for all frequencies. Penetration depth was lower for
29 milk samples with higher ash content.

30 **Keywords :** milk, dielectric properties, UHT, dielectric heating, ash content

31

32 **1. Introduction**

33 Milk is an important foodstuff for humans. Raw milk can be contaminated with
34 microorganisms that are naturally present at the animal farm and processing facilities.
35 Pasteurization and sterilization treatments are used to guarantee product safety and
36 extend shelf life. Typically, the pasteurization of milk, known as HTST (High
37 Temperature and Short Time) involves heating milk to 72 °C and maintaining this
38 temperature for 15 seconds (FAO 2004). The sterilization of milk, known as UHT
39 (ultra-heat temperature) involves heating milk to 140 °C and maintaining this
40 temperature for 1.9 seconds (FAO 2004).

41 In conventional milk processing, milk heating is achieved by transferring heat from
42 steam to the milk using heat exchangers. A problem with heat exchangers is fouling,
43 caused mainly by protein denaturization and precipitation of minerals. Fouling
44 decreases heat transfer, thus affecting milk safety if the required temperature may not be
45 achieved. Moreover, fouling increases energy consumption and the heating system must

46 be cleaned more frequently, increasing the cost of energy; labour and chemical products
47 (Gillham et al., 2000).

48 Technologies have been developed to reduce fouling problems in milk pasteurization or
49 sterilization. One of these is dielectric heating, which involves transferring heat in the
50 form of electromagnetic waves instead of through the wall of a heat exchanger
51 (convection and conduction). In food industries, the two most common dielectric
52 heating technologies use microwaves (μW) and radiofrequency (RF) waves. Some of
53 the advantages of these over conventional methods are: higher heating rates inside the
54 product that reduces processing time and energy costs; ultrafast heat treatment that
55 minimises loss of nutrients and organoleptic properties; reduced fouling deposition; and
56 higher heating efficiency and lower maintenance cost (Ahmed and Ramaswamy, 2007).
57 For instance, RF equipment from Cartigliano (Vicenza, Italy) can heat liquids up to 20
58 $^{\circ}\text{C}$ in less than 2 seconds.

59 For designing dielectric heating systems, it is important to predict how the
60 electromagnetic fields will affect the heat generation in the product. Dielectric
61 properties of a material are some of the most important parameters for this purpose
62 (Datta and Anantheswaran, 2001), the most important of which is the relative complex
63 permittivity, which can be expressed as:

$$64 \quad \epsilon = \epsilon' - j\epsilon'' \quad (1)$$

65 where,

66 ϵ is the relative complex permittivity (no units);

67 ϵ' relative real permittivity (no units), also known as dielectric constant;

68 ϵ'' is the relative loss factor (no units), also known as dielectric loss factor; and

69 j is equal to $\sqrt{-1}$.

70 The dielectric constant represents the ability of the material to store electrical energy.
71 The dielectric loss factor is related to various mechanisms of energy dissipation in
72 which electric energy is transformed into heat (Ryynänen, 1995). If heat losses are
73 insignificant, the rate of change in temperature dT/dt of any material can be calculated
74 as follows (Nelson 1996):

75
$$P = 55.63 \times 10^{-12} f E^2 \varepsilon'' \quad (2)$$

76
$$\frac{dT}{dt} = \frac{P}{c_p \rho} \quad (3)$$

77 where,

78 P is the power dissipated per unit of volume (W/m^3);

79 f is the frequency of the electromagnetic field (Hz);

80 E is the root mean square electric field intensity (V/m);

81 dT/dt is the rate of temperature increase ($^{\circ}\text{K}/\text{s}$);

82 c_p is the specific heat ($\text{J}/(\text{kg}\cdot^{\circ}\text{K})$); and

83 ρ its density (kg/m^3).

84 Dielectric permittivity changes with the temperature of the fluid and frequency of the
85 treatment waves. For this reason it is important to study the variation of dielectric
86 properties of foodstuffs with temperature and frequency.

87 Several studies on the dielectric properties of liquid foodstuffs can be found in the
88 literature. These works have studied the dielectric properties, at several temperatures
89 and frequencies, of soy sauce (Tanaka et al., 2005), fruit juices (Garcia et al, 2001; Zhu
90 at al., 2012), liquid whey protein mixture (Wang et al., 2003), and others. The dielectric
91 properties of milk have also been studied (To et al., 1974; Coronel, 2003; Nunes et al.,
92 2006; Guo et al., 2010; Zhu et al., 2014; Zhu et al, 2015a), however, not at temperatures
93 above 90°C , which are needed to predict heating in dielectric sterilization processes
94 above 100°C . The objective of this work was to study the dielectric properties of raw
95 milk (RM), skimmed milk (SM) and 35% concentrated non-fat milk (CNFM), at
96 temperatures ranging from 20 to 150°C , at a constant pressure of 4 bars, and for
97 frequencies of between 10 and 2450 MHz. These are the operating parameters of
98 conventional industrial μW and RF equipment. Special attention was given to the
99 frequencies allowed for industrial, scientific and medical (I.S.M.) applications: 27.12
100 MHz, 40.68 MHz, 433 MHz, 915 MHz and 2450 MHz.

101

102 **2. Materials and methods**

103 **2.1 Milk samples**

104 RM was purchased from a local producer (Cruilles, Catalonia, Spain). During
105 transportation, samples were kept refrigerated at 4 °C. SM was obtained from the same
106 RM sample using a skimmer (Elecrem '1', Fresnes, France) which reduced the fat
107 content to below 1%. CNFM (35% concentration) was obtained by mixing 130 liters of
108 water at 40-45 °C and 70 kg of low heat dry-milk (Lactalis Ingredients, Bougarré,
109 France) in a tank. The mixture was stirred at 156 r.p.m. for 30 minutes.

110 Table 1 shows the composition of the milk samples. For the RM and SM samples, the
111 composition was determined using a Milkoscan Minor (Type 78100, FOSS, Hillerød,
112 Denmark). For the CNFM sample, the composition was calculated from the
113 composition of dry-milk provided by Lactalis Ingredients and the percentage of added
114 water.

115

116 **2.2 Measurement of dielectric properties**

117 Dielectric measurements were performed with an open-ended coaxial-line probe (model
118 85070E) and high temperature probe, connected to a 300 KHz-20 GHz network
119 analyser (model E5071C) through an 300 kHz-26.5 GHz electronic calibration module
120 (Agilent N4691-60006). All these devices were from Agilent Technologies, Santa
121 Clara, USA. The connection between the probe and the electronic calibrator was via a
122 semi-rigid, short (14 cm long), coaxial cable special for high temperature and high
123 frequency applications, which was fan-cooled for even higher thermal stability (Micro
124 Coax UT-085C-TP-LL, Pottstown ,USA). Even at the maximum autoclave temperature
125 (150 °C), the maximum outer temperature of the cable was 60 °C at the probe connector
126 and 25 °C at the electronic calibrator connector. In that way, the electronic calibration
127 module was kept at room temperature, ensuring its correct operation. Connecting the
128 electronic calibrator and the network analyser, was a flexible μ W test cable (Mini-
129 Circuits CBL-1M-SMSM+, New York, USA). SMA gold plated, high quality RF/ μ W
130 connectors (Huber+Suhner 11_SMA-50-2-15/111_NE, Pfäffikon, Switzerland) were
131 used for all system components.

132 The Electronic Calibration Module (controlled by the Agilent 85070E probe software)
133 refreshed the calibration just prior to each measurement being made. This virtually

134 eliminated cable instability (i.e. cable movement) and system drift errors (Agilent
135 Technologies, 2012).

136 **2.3 Preliminary study of autoclave and test set-up**

137 Prior to construction of the autoclave, the placement of the probes inside the autoclave
138 and the influence of the metallic walls on the measurements was thoroughly studied.

139 The dielectric constant and the dielectric loss factor was derived from the measurement
140 of the reflection coefficient at the liquid (milk), by the coaxial transmission line (RF
141 probe) interface. Therefore, it was necessary to ensure that no other reflections disturbed
142 the measurements. Due to the shape of the RF probe (which acts as a coaxial aperture
143 antenna), reflections were caused by the autoclave wall in front of the probe.
144 Reflections from the lateral and rear walls are very small. Reflection from a metal
145 surface is higher than from the liquid – air interface. To observe the real effects of the
146 autoclave walls on the measurements, a test setup was built (Fig. 1). Metallic plates, f1,
147 f2 and f3, were situated at distances, d1, d2 and d3 respectively, from the RF probe. The
148 measuring instrument, i.e., the automatic vector network analyser Agilent E5071C
149 (Santa Clara, USA), was adjusted for continuous measurement of the reflection
150 coefficient and complex dielectric constant. Measurements were taken over a frequency
151 range of 10 – 2450 MHz with a -10 dBm RF output power. Each plate was
152 independently moved, progressively increasing the distance from the probe, until no
153 variation in the measurement was observed. The procedure was repeated with different
154 types of metallic plates (copper, aluminium), with different sizes of container (big and
155 small, made of glass), with different types of liquid (milk, distilled water), and with
156 different liquid levels (different d4 distances). The temperature probe was also placed at
157 different places near and far from the RF probe. As expected, the frontal plate (f1) was
158 responsible for the most reflection. The lateral (f2) and back (f3) plates had a very little
159 influence. The temperature probe and the liquid-air interface also had very little
160 influence on the signal.

161 The above-mentioned procedure was repeated for different temperatures (below 100
162 °C), produced using a heater (b). A thermal shield (teflon plate) was used to avoid
163 heating the electronic calibrator. It was also important to avoid the possible build-up of
164 bubbles in the milk, seriously affecting the measurements by sticking to the surface of
165 the RF probe.

166 From this initial testing, the following minimum dimensions were set for the autoclave
167 manufacture: $d_3 = d_4 = 5 \text{ mm}$; $d_2 = 10 \text{ mm}$; $d_1 = 50 \text{ mm}$. The tip of the temperature
168 probe was placed 5 mm behind and 5 mm laterally from the RF probe. This location did
169 not interfere with the RF probe measurements. The RF probe was placed horizontally to
170 minimize the risk of bubbles on the probe.

171 **2.4 Autoclave description**

172 A small autoclave (Bigas Alsina S.A, Girona, Spain) was built to enable measurement
173 of dielectric constants above 100 °C. It had a capacity of 750 ml (Fig. 2) and was built
174 in stainless steel (316 L-S), 106 mm in height and 108 mm in diameter. There were two
175 inlets for inserting the two probes (dielectric probe and the temperature probe). Both
176 inlets were 37 mm from the base and 25 mm apart. An additional inlet was available for
177 connecting a compressed air hose. The vessel could be pressurised to a constant
178 pressure during the experiment. The autoclave contents (the milk) were heated via a
179 heating jacket containing thermal oil, which was heated by an electrical resistance
180 controlled by a potentiometer..

181

182 **2.5 Experimental procedure**

183 To guarantee uniform temperature distribution throughout the sample, the sample was
184 heated very slowly by adjusting the potentiometer control. A set of dielectric
185 measurements were taken over a one-hour heating period (from 20° C to 150° C). Each
186 RF measurement (10 – 2450 MHz) took around 10 seconds. During a RF measurement
187 an increase of less than 0.1 °C (thermometer resolution) was observed with the
188 temperature probe (TESTO, Lenzkirch, Germany). This ensures a uniform temperature
189 distribution near the RF probe while measuring.

190 The experimental procedure had the following steps:

191 1) The network analyser was warmed-up for 60 minutes. The system was set-up for
192 recording 301 points across the frequency range 10 and 2450 MHz. As the measuring
193 method is less accurate at lower frequencies (10-100 MHz), many measuring points
194 were taken at lower frequency range to counter the problem.

195 2) The RF instrument was calibrated with the RF probe using the standard OSL (Open –
196 Short- Load) RF / μW calibration technique. The open circuit was obtained by leaving
197 the RF probe free in the air. The short circuit was obtained by connecting to the RF

198 probe a special add-on (supplied by the manufacturer in the Agilent 8050E probe kit,
199 Santa Clara, USA) that mechanically short-circuited the probe. The load was distilled
200 water.

201 3) The system was tested by taking measurements of distilled water at ambient
202 temperature and comparing the result with reference data.

203 4) The water was removed from the autoclave and replaced with a 500 ml sample of
204 milk. The autoclave was tightly closed and the inner pressure increased to, and
205 maintained at, 4 bar throughout the experiment, using a built-in manometer. In this way,
206 the milk did not boil when the temperature was increased to 150 °C, thus minimizing the
207 amount of water evaporated from the sample to the void.

208 5) The temperature was increased very slowly from 20 °C to 150 °C by adjusting the
209 potentiometer and monitoring it with the temperature probe.

210 6) Dielectric properties were measured every 10 °C, with two measurements taken at
211 each temperature point.

212 7) After the last measurement at 150 °C, the autoclave was left to cool to room
213 temperature (at least one hour) and then depressurized. Next, the milk removed and the
214 autoclave cleaned.

215 This procedure was repeated twice for each milk type.

216 **2.6 Penetration depth**

217 The main measurement parameters of the study were the dielectric constant ϵ' and the
218 dielectric loss factor ϵ'' . The change in these properties at different temperature and
219 frequency was evaluated. Once these properties had been derived, the penetration depth
220 of the treatment waves into milk was also derived.

221 Penetration depth (d_p) (Feynman et al., 2005) is the depth from the surface of the
222 product at which the power density has decreased by 37%. d_p (m) can be calculated
223 from the dielectric constant and loss factor using the following formula:

224

225
$$d_p = \frac{c}{2\pi f \sqrt{2\varepsilon' \left[\sqrt{1 + \left(\frac{\varepsilon''}{\varepsilon'}\right)^2} - 1 \right]}} \quad (4)$$

226 where,

227 c is the speed of the light in free space (3×10^8 m/s); and

228 f is the frequency (Hz).

229 The penetration depth parameter is useful for determining the appropriate depth of
 230 liquid which can be adequately heated using dielectric heating. According to Schiffman
 231 (1995), this should not exceed 2 or 3 times the penetration depth in order to guarantee
 232 uniform heating. d_p was derived for the three different types of milk over the same
 233 temperature and frequency ranges.

234 **3. Results and discussion**

235 **3.1 Dielectric constants**

236 The dielectric constant and loss factor for the RM, SM and CNFM samples, at
 237 frequencies of 27.12 MHz, 40.68 MHz, 433 MHz, 915 MHz and 2450 MHz, and for
 238 temperatures ranging from 20 °C to 150 °C are shown in Table 2. Fig. 3 shows the
 239 dielectric constant for RM, for frequencies ranging from 10 MHz to 2450 MHz. Similar
 240 curves were obtained for the other types of milk (figures not shown).

241 The dielectric constant decreased with frequency at all temperatures. The reduction in
 242 the dielectric constant was more pronounced for frequencies below 100 MHz. Above
 243 500 MHz, the dielectric constant tended to fall gently. This reduction was higher at high
 244 temperatures than at low temperatures. For example, for RM, at 150 °C the dielectric
 245 constant decreased from 138.9 at 27.12 MHz to 39.2 at 2450 MHz, whereas at 20 °C it
 246 decreased from 90.3 MHz to 68.6 MHz. Similar trends had previously been observed in
 247 high water content foodstuffs such as liquid whey protein mixture, cooked macaroni
 248 noodles, cheese sauce (Wang et al., 2003), smashed potatoes (Guan et al., 2004),
 249 salmon fillet (Wang et al., 2008) or fruits (Nelson et al., 2002). According to Barba and
 250 d'Amore (2012), who analysed reductions in the dielectric constant with temperature for
 251 distilled water at low frequencies, water dipoles follow the variations of the field. In this
 252 situation, dipoles store the maximum energy and the dielectric constant has the highest
 253 value. As frequency increases, the dipoles are less able to follow oscillations in the field
 254 and their storage capability decreases, decreasing the dielectric constant value. The

255 dielectric constants were similar to those of Coronel et al. (2003) at 915 MHz for
256 processed SM.

257 At the lower RF frequencies (27.12 MHz) dielectric constant tended to increase with
258 temperature, whereas at the higher μ W frequencies (2450 MHz) the dielectric constant
259 tended to decrease with temperature. According to Barba and d'Amore (2012), the
260 presence of bound water and salts makes the dielectric constant increase with
261 temperature at low frequencies. In other studies of liquid whey protein mixture and
262 cheese sauce (Wang et al., 2003), dielectric constants were also found to increase with
263 temperatures at low frequencies. This change from a decreasing to an increasing
264 response with temperature took place between 50 to 200 MHz, and varied with the type
265 of milk. Previous studies also stated that the frequency at which the change in the
266 temperature trend switches depends on the product analysed. For example, it is 55.97
267 MHz for smashed potatoes (Guan et al., 2004), 90-100 MHz for whole eggs (Wang et
268 al., 2009) or 480 MHz for bentonite water pastes (Luan et al., 2015).

269 However, this change was not observed by Zhu et al. (2012) for fruit juices in the range
270 20-4500 MHz and by Zhu et al. (2014, 2015a) for milk in the range 10-4500 MHz. In
271 these works, dielectric constant decreases with temperature across the whole range of
272 frequencies. These results were also observed for pure water (Kaatze, 1989). One
273 possible reason for the contradictory results of Zhu et al. (2014, 2015a) for milk was
274 that the glass centrifuge tubes in which the measurements were taken were too small
275 and the walls may have distorted the results. In our work, the effects of the autoclave
276 walls on the measurements were taken into consideration in the autoclave's design
277 (section 2.3).

278 At RF frequencies, the highest dielectric constants were observed for CNFM, and the
279 values for RM and SM were similar. Whereas at μ W frequencies, CNFM had the lowest
280 dielectric constants, and they were similar for RM and SM. According to Komarov et al.
281 (2005), dielectric constants decrease rapidly with decreasing moisture content, which
282 was also observed in milk (Nunes et al., 2006) at μ W frequencies. Dielectric constants
283 also tend to increase with increasing ash content at RF frequencies, whereas they tend to
284 fall with ash content at μ W frequencies. For example, for saline solutions this change
285 relative to pure water is observed at 915 MHz. At μ W frequencies, dielectric constants
286 of saline solutions decrease with temperature from 40 °C to 140 °C (Ohlsson and

287 Bengtsson, 1975). At μ W frequencies, salts (related to ash content) dissolve and form
288 ions which in turn bind the water molecules and reduce water polarization and decrease
289 the dielectric constant (Mugget, 1995). The higher ash content of CNFM may explain
290 the change in the dielectric constant for this type of milk and offset the effects of lower
291 water content of this milk. Fat and protein are relatively inert to electromagnetic waves
292 (Ryynänen, 1995; Mudgett and Westphal, 1989). Fat depresses the dielectric constant as
293 the amount of free water is reduced in the system. This might have some impact on the
294 results, but salt content is the main factor. The dielectric constant of RM was slightly
295 higher than that of SM. This difference may be explained by the slightly different
296 composition (water and ash content) of both types of milk, and the uncertainty of the
297 measurement method.

298 **3.2 Dielectric loss factor**

299 Fig. 4 shows the dielectric loss factor at different frequencies and temperatures. The loss
300 factor of the three milk types tended to decrease with frequency. For frequencies of
301 27.12 MHz, 40.60 MHz, 433 MHz and 915 MHz, the dielectric loss factor increased
302 with temperature. However, for 2450 MHz it fell gently with temperature from 20 °C to
303 60 °C and increased above 60 °C for RM and SM, whereas for CNFM it increased with
304 temperature across the whole range. At low frequencies (27.12 MHz), the dielectric loss
305 factor increased across the temperature range from 20 °C to 150 °C, by a factor of 3.6-
306 4.9, depending on the type of milk. As the frequency increased this factor tended to fall.
307 For example, at 915 MHz this factor fell to 2.8-3.6 and at 2450 MHz to 1.1-2.0. For
308 frequencies ranging from 27.12 MHz to 915 MHz these results agreed with the results
309 obtained with other foodstuffs with high water content, such as liquid whey protein
310 mixture, cooked macaroni noodles, cheese sauce (Wang et al., 2003), smashed potatoes
311 (Guan et al., 2004) or salmon fillet (Wang et al., 2008). At 2450 MHz, the dielectric
312 loss factor-temperature relationship showed a valley curve for RM and SM (Fig. 5). It
313 fell gently with temperature from 20 °C to 60 °C, and then increased again with
314 temperature. A similar behaviour was observed for low bentonite content in low
315 moisture/fat cheese (Everad et al., 2006), water paste (Luan et al., 2015) and tomatoes
316 (Peng et al., 2013). For CNFM, dielectric loss increased with temperature. A similar
317 behaviour was observed for medium and high moisture/fat cheese (Everad et al., 2006),
318 flour (Bansal et al., 2015) and saline solutions (Ohlsson and Bengtsson, 1975).
319 However, for fruit juices (Zhu et al., 2012) dielectric loss factor decreased with

320 temperature at this frequency, which differs from the behaviour observed for RM, SM
321 and CNFM.

322 With respect to other studies where the dielectric properties of milk were studied, the
323 results of this work are similar to those obtained by To et al. (1974) for aqueous non-fat
324 dry milk and Coronel et al. (2003) for skimmed milk at 915 MHz. However, results of
325 Zhu et al. (2014) and Zhu et al. (2015a) differed considerably. In these works, the
326 dielectric loss factor-temperature relationship showed a valley curve, for frequencies
327 27.12 MHz, 40.62 MHz and 915 MHz, whereas it increases clearly with temperature for
328 other foodstuffs with high water content. These results also differed from those obtained
329 by Coronel et al. (2003) for milk at 915 MHz. For 2450 MHz, dielectric loss factor
330 tended to decrease with temperature, while for most foodstuffs dielectric constant tends
331 to increase or shows a valley curve. In the previous section, these differences in the
332 dielectric responses has already been discussed.

333 According to our results, dielectric milk heating was prone to runaway heating at all the
334 frequencies studied, except for low temperatures at 2450 MHz where dielectric loss
335 increased with temperature. This means that warmer zones will heat faster, creating
336 significant temperature differences in the product (Ryynänen, 1995). This is one of the
337 most important problems of dielectric heating that contributes to overheating and
338 product quality problems. In liquids, this problem may not be so critical because of the
339 natural convection, mixing and turbulent flow conditions, which may help distribute
340 heat inside the product.

341 The behaviour of the dielectric loss factor (ϵ'') (no units) at the RF and μ W frequency
342 ranges can be explained by the combination of two phenomena, ionic conduction and
343 dipole rotation, which are the dominant loss mechanisms for foodstuffs with high water
344 content (Ryynänen, 1995):

345
$$\epsilon'' = \epsilon_d'' + \epsilon_\sigma'' \quad (5)$$

346 where

347
$$\epsilon_\sigma'' = \frac{\sigma}{2\pi f \epsilon_0} \quad (6)$$

348 By taking logarithms on both sides

349
$$\log \varepsilon''_{\sigma} = -\log f + \log \frac{\sigma}{2\pi \varepsilon_0} \quad (7)$$

350 where,

351 subscripts d and σ stands for dipole rotation and ionic conduction contributions to
352 dielectric constant, respectively;

353 σ is the ionic conductivity of the material (S/m);

354 f is the frequency in Hz; and

355 ε_0 the permittivity of the vacuum (8.854×10^{-12} F/m).

356 Ionic conduction ε''_{σ} (no units) is dominant at frequencies below 200 MHz and increases
357 with temperature, while dipole rotation ε''_d (no units) is dominant at high frequencies
358 and tends to decrease with temperature. For instance, for aqueous ionic solutions at μ W
359 frequencies, the contribution of both phenomena is similar (Roebuck et al., 1972). ε''_d
360 increases when the relaxation time of polar molecules (e.g. water) matches the
361 microwave frequency (resonance frequency). Water relaxes quicker than the resonance
362 frequency. As temperature increases, relaxation time decreases, moving farther away
363 from the resonance frequency, absorbing less energy and decreasing the value of ε''_d .
364 The increase of ε''_{σ} with temperature is explained by the reduced viscosity and increased
365 mobility of ions (Tang, 2005). According to Luan et al. (2014), the combination of these
366 two loss mechanisms may explain the valley curve for the dielectric loss constant
367 observed at 2450 MHz in this study (Fig. 5).

368 According to Eq. 5, frequency and the dielectric loss factor will show a linear
369 relationship in a log-log graph if dielectric loss ε'' is dominated by ionic conduction
370 (ε''_{σ}). The second term on the right side of the equation is constant because conductivity
371 is constant for a given temperature. In Fig. 4, where dielectric loss factor versus
372 frequency is depicted in a log-log graph, there is a linear relation with a negative slope
373 from 15 MHz to around 800 MHz for all the studied temperatures. Above 800 MHz,
374 dipole rotation losses start to contribute more to the dielectric loss, and ionic loss
375 contribution starts to decrease. This result suggests that ionic conduction is the
376 dominant loss mechanisms in the low range of frequencies.

377 CNFM shows the highest value of dielectric loss factor at low and high frequencies,
378 much higher than that of RM and SM. The reason for this is the higher ash content
379 (related to salt content) which substantially increases the dielectric loss factor (Komarov
380 et al., 2005). Fat content of CNFM milk is only 0.23% compared with 3.55% for RM
381 and 0.63% for SM. The higher fat contents of the RM and SM samples may have
382 contributed to this result as well. According to Zhu et al. (2015b), fat occupies a volume
383 in the conducting medium and impedes the movement of conducting ions at frequencies
384 below 300 MHz, lowering conductivity and the dielectric loss factor. SM presents in
385 general a higher dielectric loss factor than RM. However, ash concentration seems to
386 dominate the heat generation. Zhu et al. (2015b), Coronel et al. (2003) and Nunes et al.
387 (2006) observed similar results for raw and skimmed milk at 915 MHz and above 1
388 GHz, respectively.

389 **3.3 Penetration depth in milk**

390 The derived penetration depths for the studied milk types are shown in Figs. 6 to 8. As
391 expected, the penetration depth decreased with frequency and temperature, but only
392 slightly at high frequencies. Penetration at 20 °C ranged from as much as 120 mm at RF
393 frequencies to 20 mm at μ W frequencies for RM, decreasing by a factor of 1/6. For the
394 temperature range under consideration, penetration depth for RF frequencies decreased
395 by as much as a factor of 1/2 from around 120 mm at 20 °C to 60 mm at 150 °C. This
396 decrease was much lower in the μ W range as penetration depth showed small changes
397 with temperature. Values for RM were slightly higher than for SM. CNFM presented
398 much lower values than RM and SM. In general, foodstuffs penetration depth decreases
399 with salt content, for example in potatoes (Guan et al., 2004).

400 The effect of frequency was more important than that of temperature. This behaviour is
401 similar to that observed for whey proteins, cheese sauce and macaroni (Wang et al.,
402 2003), fruit juices (Zhu et al., 2007), salmon (Wang et al., 2008), among others. A
403 similar response to changes in frequency was observed for milk by Zhu et al. (2014),,
404 but with no clear trend for temperature change, which is unlike this study and other
405 previously mentioned studies.

406 From these results, it can be concluded that pipe diameter for continuous treatment (up
407 to 150 °C) should not exceed approximately 120 mm for RF dielectric heating and 20

408 mm for μ W heating for RM and SM (Schiffmann, 1995). For CNFM these values are
409 much lower, 80 mm for RF and 7.5 mm for μ W.

410 **4. Conclusions**

411 Dielectric properties of milk above 100 °C can be successfully determined. This was a
412 novel finding in the study of the dielectric properties of milk. Dielectric properties are
413 affected by the composition of milk, in particular the water and ash content (related to
414 salt content). Ash content is the most important factor. Milk is prone to runaway heating
415 across a wide range of frequencies. This poses a problem for RF thermal treatment of
416 milk, but is not a problem for μ W thermal treatment. RF dielectric heat treatment allows
417 the use of pipes with larger diameters than μ W treatment due to the higher penetration
418 depth of RF.

419 **Acknowledgments**

420 The research leading to these results has received funding from the European Union's
421 Seventh Framework Programme under grant agreement n° 613732, "Enthalpy" and
422 CERCA programme from Generalitat de Catalunya.

423 The authors thank Marta Garrón, Grau Matas and Cristina Canals for their valuable
424 technical assistance.

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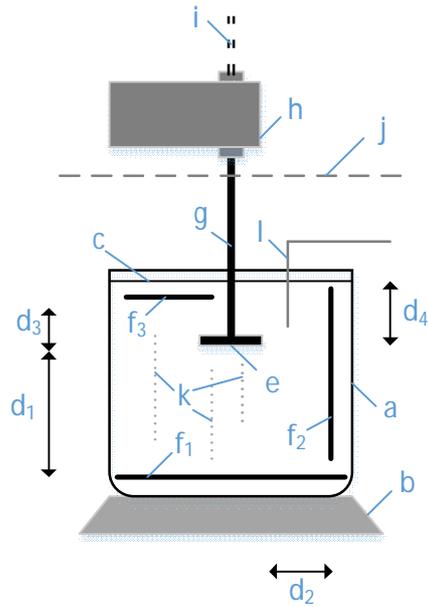
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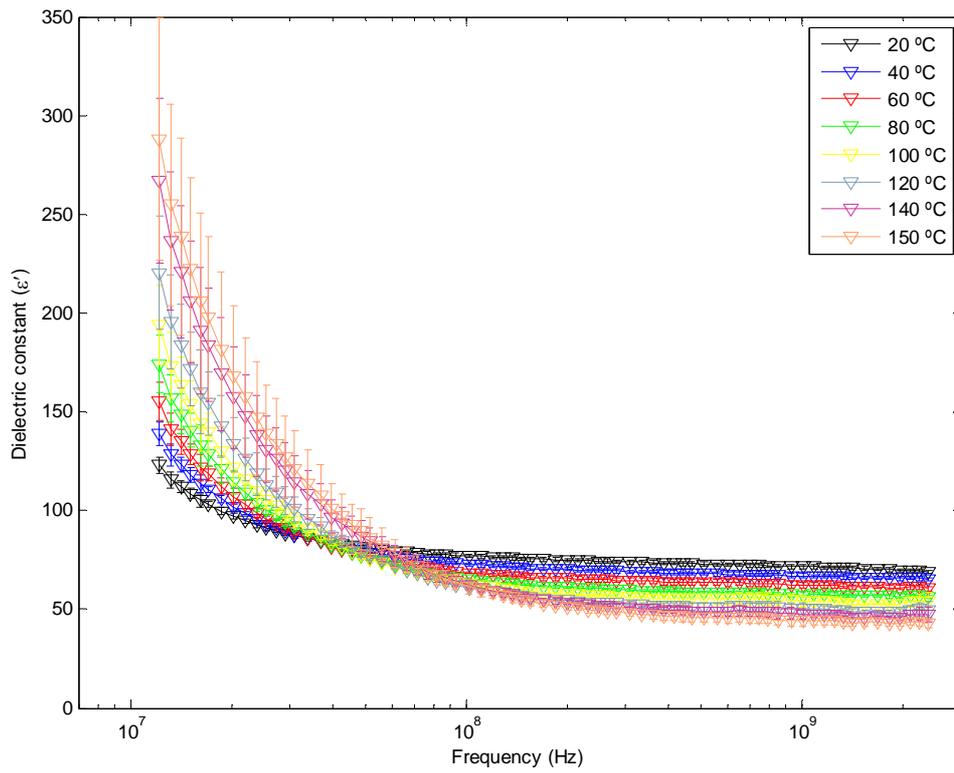
521 Fig. 1. Schematic drawing of test setup (not to scale). a: container; b: heater; c: liquid
 522 (milk, distilled water) test level; d_1 : distance from the RF probe to a frontal metallic
 523 plate; d_2 : distance from the RF probe to a lateral metallic plate; d_3 : distance from the RF
 524 probe to a back metallic plate; d_4 : distance from the RF probe to the liquid-air interface;
 525 e: RF probe; f_1 : movable frontal metallic plate; f_2 : movable lateral metallic plate; f_3 :
 526 movable back metallic plate; g: rigid coaxial transmission line; h: electronic calibrator;
 527 i: flexible coaxial transmission line; j: thermal shield; k: possible bubbles; l: temperature
 528 probe.



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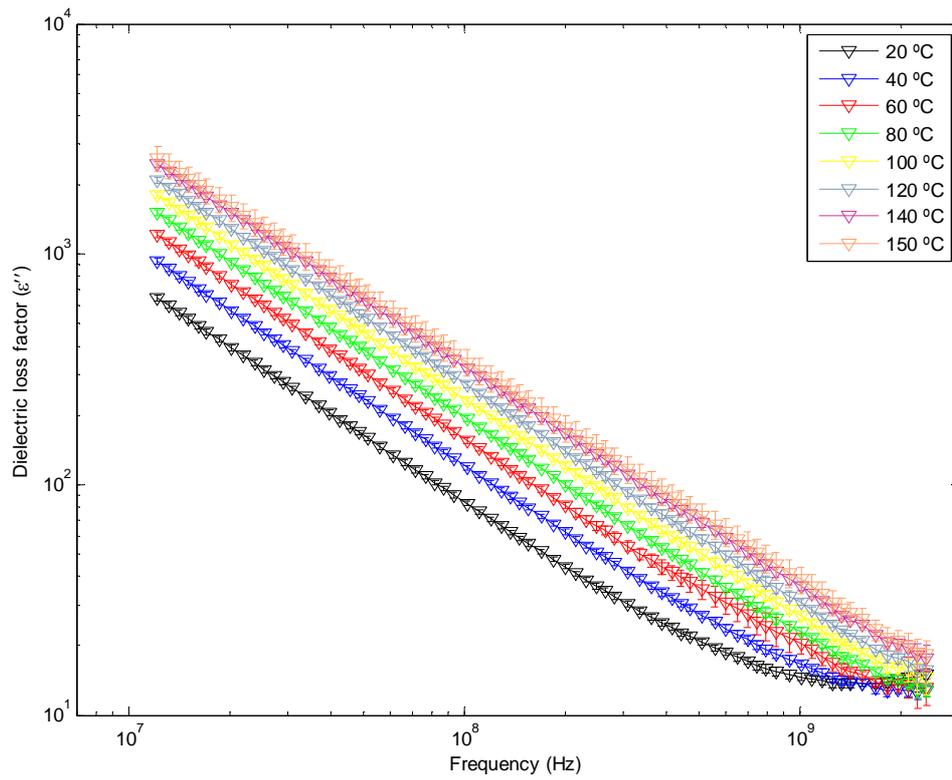
Fig. 2. Autoclave for measuring the dielectric constant.



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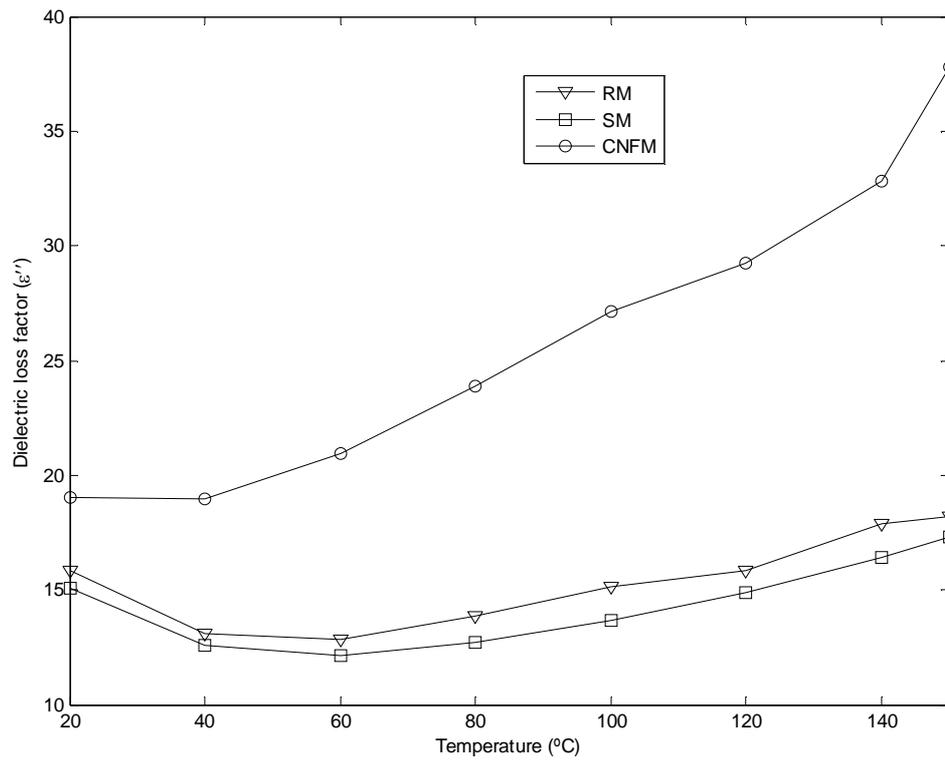
532 Fig. 3. Dielectric constants of raw milk in the 10 MHz to 2450 MHz frequency range at
 533 the indicated temperatures.

534

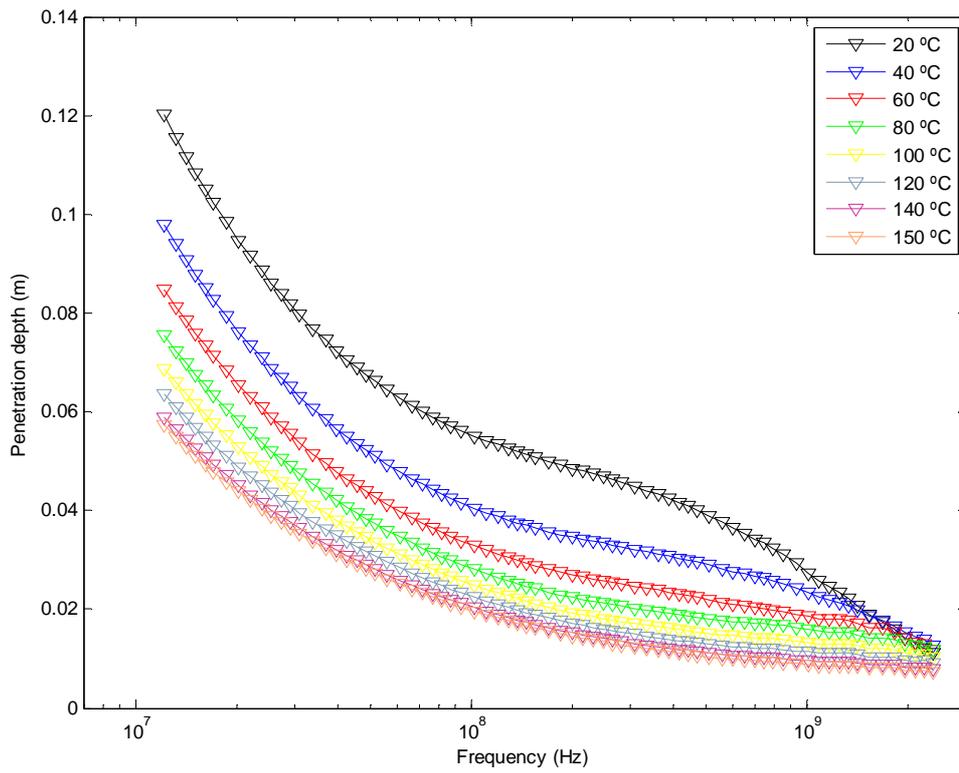


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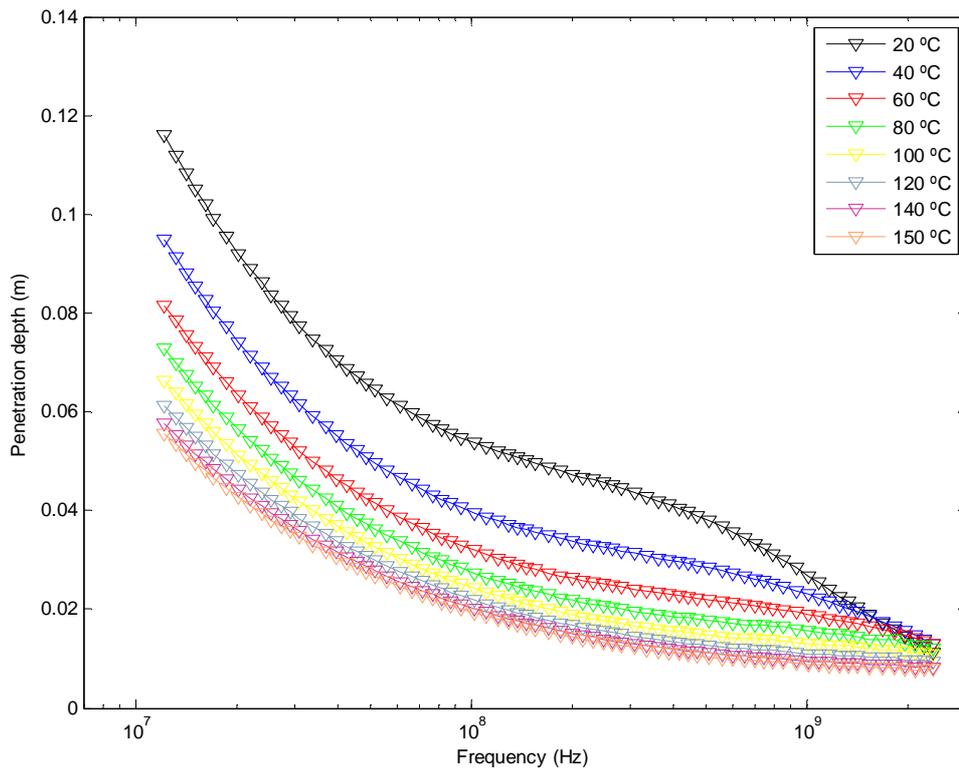
536 Fig. 4. Dielectric loss factor of raw milk in the 10 MHz to 2450 MHz frequency range at
 537 the indicated temperatures.



538
 539 Fig. 5. Dielectric loss factor of three types of milk (RM, SM and CNFM) at 2450 MHz
 540 and at temperatures from 20 °C to 150 °C.



541
 542 Fig. 6. Penetration depth of raw milk in the 10 MHz to 2450 MHz frequency range at
 543 the indicated temperatures.

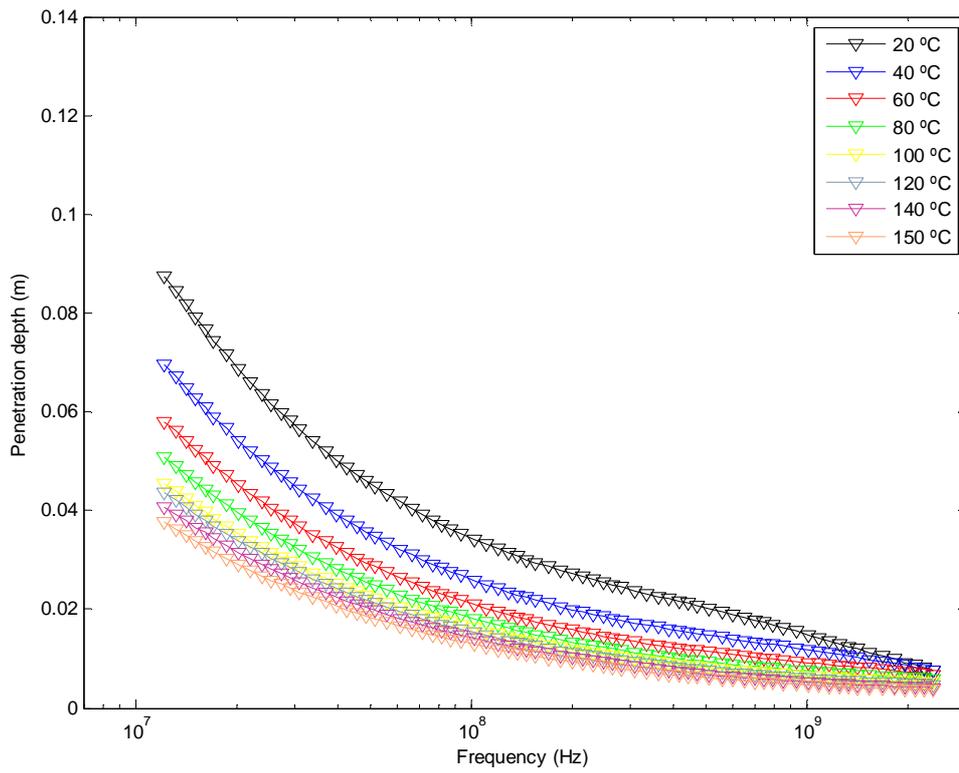


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546 Fig. 7. Penetration depth of skimmed milk in the 10 MHz to 2450 MHz frequency range

547 at the indicated temperatures



548

549 Fig. 8. Penetration depth of concentrated non-fat milk in the 10 MHz to 2450 MHz
 550 frequency range at the indicated temperatures.

Type of milk	Water (%)	Fat (%)	Protein (%)	Lactose (%)	Ash (%)
RM	88.20 ± 0.06%	3.55 ± 0.02%	3.24 ± 0.04%	4.68 ± 0.02%	0.32 ± 0.06%
SM	90.44 ± 0.03%	0.99 ± 0.00%	3.29 ± 0.00%	4.68 ± 0.00%	0.6 ± 0.01%
CNFM	65.45 ± 0.00%	0.23 ± 0.00%	11.99 ± 0.00%	19.39 ± 0.00%	2.94 ± 0.00%

551 Table 1. Milk composition of RM, SM and CNFM samples (mean ± standard deviation)

552

Milk type	Frequency (MHz)		Temperature (°C)								
			20	40	60	80	100	120	140	150	
RM	27.12	ϵ'	90.4±0.1	91.6±1.0	93.3±1.3	97.7±2.7	102.3±4.5	109.3±7.9	125.6±15.8	133.7±22.3	
		ϵ''	299.8±7.3	432.7±11.2	562.6±10.8	706.6±19.8	843.7±24.3	979.8±29.9	1150.2±34.6	1088.5±119.3	
	40.68	ϵ'	83.3±1.0	81.4±1.3	80.0±2.1	80.5±2.6	81.6±3.5	84.5±4.6	94.2±7.7	99.6±12.1	
		ϵ''	203.6±4.7	292.0±7.9	379.8±12.2	476.9±14.4	569.7±18.1	661.9±22.7	780.7±25.8	830.5±84.9	
	433	ϵ'	73.6±0.8	68.3±1.0	63.1±1.1	58.8±0.8	55.5±2.0	51.6±1.7	49.3±1.7	46.4±2.0	
		ϵ''	23.4±0.6	31.3±1.0	39.4±0.5	49.0±1.7	58.5±2.4	67.6±2.8	80.2±3.6	85.1±9.9	
	915	ϵ'	72.8±1.5	67.6±1.6	63.4±3.3	59.7±5.3	55.6±3.8	51.4±3.3	48.7±3.3	44.4±2.6	
		ϵ''	15.3±0.4	17.7±0.7	20.7±0.7	25.0±1.1	29.5±1.8	33.4±1.5	39.3±1.7	42.0±5.2	
	2450	ϵ'	70.3±2.2	66.2±2.2	62.7±4.9	59.7±7.8	55.0±4.5	51.2±4.5	48.3±4.3	43.0±2.1	
		ϵ''	15.9±0.6	13.1±0.7	12.9±1.2	13.9±2.1	15.1±2.1	15.9±1.6	18.0±1.8	18.2±2.0	
	SM	27.12	ϵ'	89.7±2.7	90.0±3.4	91.1±4.2	93.4±4.7	96.5±5.1	102.0±5.4	113.8±5.7	119.8±6.2
			ϵ''	310.0±2.0	447.1±4.5	590.6±3.4	732.2±3.6	873.5±5.9	1020.2±6.2	1159.7±11.8	1239.4±19.2
		40.68	ϵ'	84.5±1.9	82.1±2.2	80.6±2.8	80.5±3.2	81.0±3.4	83.3±3.9	90.0±4.6	93.6±5.1
			ϵ''	209.4±1.5	301.9±3.6	399.0±2.9	494.7±2.3	590.5±4.8	690.1±5.2	785.9±7.6	842.8±12.3
433		ϵ'	75.2±0.9	70.0±0.8	64.8±0.8	60.0±1.0	55.7±0.8	51.8±0.9	49.0±1.0	47.5±2.5	
		ϵ''	24.3±0.4	32.2±0.6	41.0±0.4	50.0±0.3	59.5±0.8	69.7±1.1	79.8±1.3	85.2±1.4	
915		ϵ'	73.7±1.1	68.6±0.9	63.5±0.9	58.7±1.1	54.3±0.9	50.3±1.0	47.2±1.1	45.6±2.7	
		ϵ''	15.7±0.6	18.2±0.6	21.7±0.5	25.4±0.4	29.6±0.6	34.4±1.0	39.1±1.2	41.8±1.0	
2450		ϵ'	71.2±0.9	67.0±0.8	62.3±0.8	57.5±1.1	53.3±0.8	49.2±1.0	46.0±1.0	44.4±2.7	
		ϵ''	15.1±0.6	12.6±0.5	12.1±0.6	12.7±0.4	13.6±0.5	14.9±0.5	16.4±0.5	17.3±0.5	
CNFM		27.12	ϵ'	99.1±2.9	108.0±3.3	119.6±5.4	131.9±7.0	143.7±8.2	151.9±4.5	178.4±13.2	204.3±19.3
			ϵ''	536.8±1.9	791.0±33.3	1121.6±24.2	1454.3±28.2	1801.5±110.2	1953.5±34.6	2265.9±35.7	2656.9±23.8
		40.68	ϵ'	87.5±0.6	92.5±0.8	99.0±1.8	106.2±2.5	112.7±2.1	117.6±0.0	133.4±5.6	148.6±9.1
			ϵ''	365.6±1.5	537.1±22.9	760.0±17.1	983.9±20.4	1213.2±66.5	1319.2±27.5	1531.6±25.9	1795.7±18.1
	433	ϵ'	61.6±1.5	60.4±1.2	58.7±1.2	57.0±1.1	56.6±0.2	55.5±0.4	53.4±1.6	53.4±1.2	
		ϵ''	43.8±0.5	60.3±2.3	82.3±1.7	104.6±2.0	125.7±3.6	138.2±4.3	160.8±2.6	188.0±2.1	
	915	ϵ'	57.7±1.4	56.2±1.2	54.1±1.1	52.0±1.0	51.3±0.3	49.6±0.3	46.4±1.4	45.5±1.1	
		ϵ''	26.3±0.6	33.1±1.2	43.0±0.9	53.4±1.0	63.1±1.2	69.2±2.4	80.0±1.3	92.9±1.2	
	2450	ϵ'	51.8±1.3	51.6±1.5	49.8±1.5	47.7±1.3	47.2±0.3	45.4±0.1	41.9±1.8	40.9±1.4	
		ϵ''	19.0±1.1	19.0±1.0	20.9±0.9	23.9±0.9	27.1±0.1	29.2±1.4	32.9±1.0	37.8±0.9	

553 Table 2: Dielectric constant (ϵ') and loss factor (ϵ'') (mean \pm standard deviation) of three different types of milk (raw milk (RM), skinned milk
554 (SM) and concentrated non-fat milk (CNFM)) at 5 frequencies (ISM Bands) and 8 temperatures.