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25 **ABSTRACT**

26 Predictive modeling of dielectric heating in porous foods is challenging due to their nature as multiphase
27 materials. To explore the relationship between the topological structure of multiphase foods and the
28 accuracy of dielectric mixture models, the degree of anisotropy of two cooked rice samples with 26 and
29 32 % porosity was determined, and their dielectric properties were estimated using the Lichtenecker (LK),
30 Landau-Lifshitz-Looyenga (LLL), and Complex Refractive Index Mixture (CRIM) equations. These
31 properties were used in a predictive finite-element model for reheating an apparent homogeneous rice
32 sample on a flatbed microwave (MW) for 120 s. The results were compared with experimental data and
33 a validated two-element model. Unlike LK and LLL equations, the CRIM equation predicted heat
34 accumulation towards the edges of the container at the two values of porosity ratio evaluated, in
35 accordance with the experimental results and the isotropic nature of the sample. The simulated
36 temperature distributions suggest that the three evaluated equations could predict the MW heating
37 behavior of rice to some extent, but that in order to obtain more accurate results, it could be useful to
38 obtain an empirical topology-related parameter specific for this sample. These results can provide insight
39 on the relationship between the topology of the porous structure in the sample and the adequacy of
40 different dielectric mixture models.

41

42 **KEYWORDS:** Microwave; packed rice; porosity; dielectric mixture equations; anisotropy; computer
43 simulation

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49 1. INTRODUCTION

50 In recent years, lifestyle changes have led to an increased consumption of ready-to-eat meals, propelling
51 the convenience food industry to surpass the trillion-dollar mark globally (Yadav et al., 2024).
52 Consequently, microwave (MW) heating has been positioned as an indispensable tool, not only for
53 reheating convenience meals in the household but also for their commercial sterilization in the industry
54 (Auksornsri et al., 2018).

55 When developing ready-to-eat foods or designing industrial thermal treatments, assessing temperature
56 distributions is critical to identifying hot and cold spots and understand their dependence on factors such
57 as formulation or operational parameters (Auksornsri et al., 2018). This is often challenging and resource-
58 intensive, especially when relying on trial-and-error approaches. In this context, computer simulation
59 offers an advanced solution for analyzing heating behavior in domains that are difficult to study
60 experimentally (Zhang et al., 2024).

61 Rice is a common ingredient in ready-to-eat foods (Auksornsri et al., 2018). It consists of a porous matrix
62 with air and rice phases of varying volume fractions. Simulating MW heating of such foods presents
63 unique challenges due to varying dielectric properties among different phases (Sawale et al., 2024).
64 Although there are methods to measure the dielectric properties of heterogeneous materials, each has its
65 own limitations. For instance, the resonant cavity method is commonly applied but its accuracy is limited
66 to low-loss materials such as oils and plastics (Zhou et al., 2024).

67 One way to address this challenge is to use dielectric mixture equations. A common form of these models
68 is presented in its general form in Eq. 1, for a mixture of N phases.

$$\varepsilon = \left(\sum_{i=1}^N V_i \varepsilon_i^\alpha \right)^{\frac{1}{\alpha}} \quad (1),$$

69 where ε represents the complex dielectric permittivity ($\varepsilon = \varepsilon' - j\varepsilon''$) of the mixture (-), V_i and ε_i are
70 the volume fraction (-) and complex permittivity (-) of each of the phases, respectively, and α is a
71 topology-dependent parameter (-) which ranges between 1 and -1.

72 The values of $\alpha = -1$ and $\alpha = 1$ in Eq. 1 are known as the Wiener bounds and describe situations of
73 anisotropy where all layers or pores are perpendicular or parallel to an applied external electric field,
74 respectively (Zakri et al., 1998). Between these bounds, for mixtures with a certain level of isotropy in
75 their pore structure, different values of α have been arrived at from different theoretical approaches.

76 Assuming $\alpha = 0$ for a mixture of two phases a and b , Eq. 2 is obtained:

$$\ln\varepsilon = V_a \ln\varepsilon_a + V_b \ln\varepsilon_b \quad (2).$$

77 This is often referred to as Lichtenecker's (LK) equation, it was obtained from a semi-empirical basis by
78 Lichtenecker & Rother (1931). Nonetheless it has been applied over the years in multiphase materials
79 and theoretical evidence for it has been provided in recent times (Goncharenko et al., 2000; Simpkin,
80 2010; Zakri et al., 1998) .

81 Eq. 3 is obtained by assuming $\alpha = 0.5$:

$$\sqrt{\varepsilon} = V_a \sqrt{\varepsilon_a} + V_b \sqrt{\varepsilon_b} \quad (3).$$

82 This is commonly called the Complex Refractive Index Mixture (CRIM) equation (Birchak et al., 1974),
83 and it has been arrived at by a number of researchers considering wave propagation through a
84 heterogeneous dielectric mixture. It has a proper theoretical basis when considering the relationship
85 between the complex permittivity of a medium, and the real part of the refractive index of a single
86 electromagnetic wave, which determines the propagation velocity (Birchak et al., 1974; Kraszewski,
87 1977; Whalley, 1993).

88 Other values of α have been derived, such as $\alpha = 0.33$ in the case of the Landau-Lifshitz-Looyenga
89 (LLL) equation (Looyenga, 1965):

$$\sqrt[3]{\varepsilon} = V_a \sqrt[3]{\varepsilon_a} + V_b \sqrt[3]{\varepsilon_b} \quad (4).$$

90 This equation, often cited as assuming a spherical topology, is well known for its versatility and accuracy
91 specially at high frequencies (Khan et al., 1986; Nelson & You, 1990; Nelson, 2000).

92 Literature dealing with the use of dielectric mixture equations on food products is relatively scarce.
93 Nelson (2005) used different equations to explore the relation between the permittivity of granulated
94 wheat and flour samples and their bulk density, (Liu et al., 2009) used them to obtain the dielectric
95 properties of porous bread considering it a mixture of compact bread and air. Alfaifi et al. (2014)
96 compared different equations in terms of the accuracy to estimate the dielectric properties of a raisins-air
97 two-phase porous system. More recently, they were used by Chen et al. (2019) to simulate radiofrequency
98 heating of a mixture of egg white powder and air, by Yan et al. (2023) to simulate MW heating of a
99 surimi, air, and water mixture, and by Zhang et al. (2024) to estimate the dielectric properties of crushed
100 ice. However, the simulation accuracy at more than one volume fraction was not investigated.

101 In our previous study (Taguchi et al., 2025), a simulation model for MW heating of cooked rice was
102 developed and validated. However, this model involves dividing the sample domain into rice or air
103 elements, each with distinct physical properties. This can be time-consuming and impractical for certain
104 multiphase foods. Therefore, the aim of the present study is to use this validated model to study the
105 applicability of various mixture equations for estimating the dielectric properties of an apparent
106 homogeneous cooked rice sample. This can provide insight on different ways of accurately predicting
107 the behavior of porous foods during dielectric heating in more effective manner. The specific objectives
108 are:

- 109 - To develop MW heating simulation models of cooked rice using an apparent homogenous food
110 approach with different dielectric mixture equations and porosity ratios.

- 111 - To compare the temperature distributions predicted with various dielectric mixture equations at
112 two different porosity ratios.
- 113 - To explore the relationship between the topological structure of the samples and the accuracy of
114 different dielectric mixture equations at varying porosity ratios.

115

116 **2. MATERIALS AND METHODS**

117 **2.1 Sample preparation**

118 To ensure the homogeneity of the samples used in the experiments, cooked commercial packed rice (Var.
119 Koshihikari, TopValu, Japan) was used. For the heating experiments, the rectangular polypropylene (PP)
120 containers in which the samples are commercially sold were used, since these containers are typically
121 used by consumers to heat the samples at home. To quickly obtain thermal images of the sample's cross
122 section after the experiments, the containers were cut in half along their longitudinal axis. The dimensions
123 of the container and the longitudinal sections are shown in Fig. 1. The two parts were stuck together with
124 heat-resistant tape and the containers were filled with different quantities of cooked rice. Finally, a 0.1
125 mm polyethylene (PE) film was glued to the top using a household iron.

126

127 **2.2 Heating experiments**

128 In each experiment the same volume of rice was used, obtained by gently mashing 326 g or 300 g until
129 the original level present in the commercial product was reached, to obtain rice with 26 or 32 % porosity,
130 respectively. These values were chosen based on preliminary trials where porous ratios of ready-to-eat
131 rice from different brands and traditionally prepared rice using a rice cooker were measured. The
132 following relationship was used to obtain the quantity of cooked rice corresponding to each porosity (Li
133 et al., 2019):

$$\phi = 1 - \frac{w_r}{\rho_r V_c} \quad (5),$$

134 where ϕ is the porosity ratio ($-$), w_r and ρ_r are the weight (kg) and density (kg/m^3) of rice,
135 respectively, and V_c is the total volume of rice in the container (m^3). Photographs of the sample's
136 longitudinal cross-section can be seen in the supplementary data of this article (Fig. S1).

137 Prior to heating, the samples were kept at a constant temperature of 20 °C for 6 hours, using a thermostatic
138 chamber (DKN602, Yamato Scientific, Japan). Two optic fiber sensors (FS100-2M, Anritsu, Japan) were
139 inserted into the sample through the PP film according to the positions shown in Fig. 2.

140 Then, the samples were heated at 600 W for 30 s, 60 s, 90 s, and 120 s using a household flatbed MW
141 oven (MRO-CF6, Hitachi, Japan). This type of oven, commonly used in Japanese households, is
142 equipped with a stirring aluminum antenna that distributes the electric field to obtain varying
143 distributions inside the cavity, eliminating the need for a turntable. The frequency was specified as the
144 nominal value of 2450 MHz and the MW oven and its magnetron were totally cooled down with a fan
145 between experiments.

146 Finally, the heat-resistant tape was removed, and thermal images were taken using a previously calibrated
147 infrared camera (TH7102WV, NEC San-ei Instruments Inc., Japan) supported by the InfReC Analyzer
148 NS9500 Standard software (Nippon Avionics Co Ltd., Japan). Experiments at each heating time were
149 carried out in triplicate.

150

151 **2.3 Determination of the porosity and degree of anisotropy**

152 The porosity ratio of each sample was then confirmed using an X-ray computed tomography (CT)
153 scanner (Sky scan 1172 microCT, Bruker, Belgium) to obtain X-ray images of the rice samples. A small
154 cylindrical portion of rice (2.5 cm in diameter \times 2 cm in height) was carefully taken from the container
155 and placed in a sample holder with a diameter of 4.5 cm in order to avoid disrupting the internal pore

156 structure and affecting the porosity. The samples were then scanned under an X-ray source of 59 kV and
157 100 μ A, with a stage rotation of 180 $^\circ$ rotations with 0.4 $^\circ$ rotation steps. A total of 1200 projections per
158 sample were obtained using a CCD camera with an image pixel size of 13.59 μ m.

159 The image reconstruction was carried out using the NRecon Skyscan (Bruker, Belgium) software. The
160 software produced two-dimensional axial images with a resolution of 2000 x 2000 pixels. The grayscale
161 pixel values for pure black and white were recorded to be 0 and 255, respectively. The porosity ratio and
162 the degree of anisotropy were then calculated using the CTAn software (Bruker, Belgium).

163 The degree of anisotropy was calculated using the mean intercept length (MIL) method, where vectors
164 are generated from a random point in the sample, then the MIL from that point are obtained by dividing
165 the length of the vector by the number of hits with a rice/pore intersection. Further, a material anisotropy
166 tensor is established by fitting the MILs to an ellipsoid and the degree of anisotropy is obtained as:

$$\text{Degree of anisotropy} = 1 - \frac{E_s}{E_l} \quad (6),$$

167 where E_s and E_l are the smallest and largest eigenvalues of the material anisotropy tensor (Yu et al.,
168 2021).

169

170 **2.4 Predictive model**

171 **2.4.1 Model geometry**

172 A commercial FEM software, FEMAP (Ver 10.2 Siemens PLM Software Inc., USA) was used to create
173 the 3D geometric model of the flatbed MW oven and the sample identically to the real geometries (Fig.
174 3) with the exception of the waveguide. The actual oven has a TE₁₀ (height: 35 mm, width: 85 mm)
175 rectangular waveguide, but to reduce the calculation time the coaxial space at the bottom of the cavity
176 was considered an equivalent coaxial waveguide for the simulation using the method described by Liu
177 et al. (2014a). The heat transfer and electromagnetic equations were solved using the Thermo-HT and

178 the Wavej ω -EM modules of the commercial software PHOTO-series (Ver. 7.2, PHOTON Co. Ltd.,
179 Japan) respectively.

180 Two different approaches for the sample model were explored. The first approach was to create a two-
181 element domain using a FORTRAN routine to randomly convert a certain number of rice elements in the
182 sample to void elements, according to the porosity ratios obtained in section 2.2. This method was
183 explained in detail in (Taguchi et al., 2025). The second approach was to consider the sample as an
184 apparent homogeneous dielectric mixture. In this case, each element in the sample domain was assigned
185 the physical properties. Both approaches are illustrated in Fig. 4.

186

187 2.4.2 Governing equations

188 The electromagnetic field distribution in space and time is calculated using Maxwell's equations, which
189 are shown below in their differential form (Curet et al., 2008):

$$\nabla \cdot \vec{B} = \nabla \cdot \mu \vec{H} = 0 \quad (7)$$

$$\nabla \cdot \vec{D} = \nabla \cdot \epsilon \vec{E} = \rho_m \quad (8)$$

$$\nabla \cdot \vec{H} = \frac{\partial \vec{D}}{\partial t} + J = \frac{\partial \epsilon \vec{E}}{\partial t} + \sigma \vec{E} \quad (9)$$

$$\nabla \cdot \vec{E} = -\frac{\partial \vec{B}}{\partial t} = -\frac{\partial \mu \vec{H}}{\partial t} \quad (10),$$

190 where \vec{B} is the magnetic induction (Wb/m^2), \vec{H} is the magnetic field intensity (A/m), \vec{D} is the electric
191 field displacement (C/m^2), \vec{E} is the electric field intensity (V/m), ρ_m is the electric volume charge
192 density (C/m^3), t is the time (s), J is the current flux (A/m^2), ϵ is the complex permittivity ($\epsilon = \epsilon' -$
193 $j\epsilon''$) ($-$), and μ is the magnetic permeability (H/m).

194 The conversion of electromagnetic energy to thermal energy Q (W/m^3) is given by Poynting's theorem
195 (Birla et al., 2008; Choi & Konrad, 1991):

$$Q = 2\pi f \varepsilon_0 \varepsilon'' |\vec{E}|^2 \quad (11),$$

196 where ε'' is the dielectric loss factor ($-$), f is the MW frequency (1/s), and ε_0 is the permittivity of
 197 vacuum ($8.854 \times 10^{-12} \text{ J}/(\text{V}^2 \text{ m})$). The total heat balance in the model is governed by Fourier's
 198 equation (Lan et al., 2020):

$$\rho C_p \frac{\partial T}{\partial t} = \nabla(k\nabla T) + Q \quad (12),$$

199 where C_p is the specific heat ($\text{J}/(\text{kg K})$), T is the temperature (K), and k is the thermal conductivity
 200 ($\text{W}/(\text{m K})$).

201

202 **2.4.3 Assumptions**

203 The aforementioned equations were solved under the following assumptions:

- 204 - Given that the samples were kept at a constant temperature and the MW oven was cooled down
 205 between experiments, the initial temperature within each domain was assumed as uniform.
- 206 - Since no thermal expansion or shrinkage of the samples was observed, and it is not expected to
 207 notably affect the trend of transport phenomena in the porous media, it was neglected (Shen et
 208 al., 2022).
- 209 - The samples were assumed to behave non-magnetically so their permeability was set to that of
 210 vacuum ($\mu_0 = 4\pi \times 10^{-7} \text{ H}/\text{m}$) (Curet et al., 2008).
- 211 - The research focus lied on exploring the adequacy of the dielectric mixture models and the
 212 topology of the samples, so phase change and moisture loss were not modeled (Ye et al., 2021).
- 213 - The frequency was assumed to be the nominal value of 2450 MHz. While it can vary slightly
 214 across equipment and change with time, load position, or dielectric properties, this variability was
 215 considered negligible (Chan and Reader, 2000).

216

217 **2.4.4 Initial and boundary conditions**

218 The following boundary conditions were applied for the governing equations in the predictive model:

219 - Slide interfaces were assigned to the contact surfaces between rotating and stationary parts (Liu
220 et al., 2014a).

221 - The initial temperature T_i ($^{\circ}C$) of all the domains in the model was set to $20^{\circ}C$ in all simulation
222 runs:

$$T = T_i \text{ at } t = 0 \quad (13).$$

223 - The oven walls were assumed to be thermally insulated:

$$\nabla T = 0 \quad (14).$$

224 - The oven walls, coaxial waveguide, and antenna surface were set as perfect electrical conductors,
225 since they are metallic materials expected to reflect electromagnetic radiation almost entirely,
226 resulting in zero normal components of the magnetic and electric fields (Llave et al., 2020):

$$H_n = 0, E_n = 0 \quad (15).$$

227

228 **2.5 Solution method**

229 **2.5.1 Time stepping for rotation**

230 The rotation speed of the stirring antenna was set to $120^{\circ}/s$. A time step of 6.666 s was used, which
231 corresponds to a rotation update interval of 400° . This value was chosen to maximize the accuracy of
232 the model by allowing for 9 calculation steps per cycle according to the antenna rotation speed and the
233 duration of the experiments. The same approach was used by Liu et al. (2014a) for the heating of mashed
234 potatoes on a flatbed MW oven. A schematic diagram of the main simulation steps can be found in
235 (Taguchi et al., 2025).

236

237 **2.5.2 Calculation of absorbed power**

238 At each time step, the heat transfer module distributes a value of absorbed power according to the electric
239 field distribution obtained by the electromagnetics module. The power absorbed by the samples
240 corresponded to 379.5 W, this value was obtained using a variation of the International Electrotechnical
241 Commission method (IEC, 2014) proposed by Pitchai et al. (2012): 2000 mL of distilled water were
242 heated for 120 s at 600 W (nominal power). The final temperature was recorded and the power
243 absorption Q (J) was calculated as follows:

$$\frac{WC_p\Delta T}{\Delta t} = Q \quad (16),$$

244 where W corresponds to the mass of water (kg) and C_p to its specific heat (4178 J/(kg K)) (Choi &
245 Okos, 1986). This method has been applied in a number of studies dealing with MW heating of foods
246 (Kako et al., 2022; Liu et al., 2014b; Yan et al., 2023) and assumes a constant value of absorbed power
247 independent of the dielectric properties of the materials.

248

249 **2.5.3 Mesh size determination**

250 The model consisted exclusively of hexahedral-shaped elements. The appropriate mesh-size h (mm)
251 relative to the MW wavelength λ (mm) and the relative dielectric constant ε' (–) was determined from
252 Eq. 17 (Liu et al., 2013). The total number of elements in all domains was 242236.

$$h = \frac{\lambda}{6\sqrt{\varepsilon'}} \quad (17).$$

253 All modeling calculations were performed on a workstation with an Intel(R) Core (TM) i7-7700
254 processor (CPU speed: 3.6 GHz) and 8.00 GB RAM. The calculation time was approximately one week
255 for the two-element model and slightly less than that for the apparent homogeneous models. The meshing

256 for each individual domain of the model geometry can be found in the supplementary data of this article
257 (Fig.S2).

258

259 **2.6 Determination of thermophysical and dielectric properties**

260 Temperature-independent thermophysical and dielectric properties of air, PP, and ceramic were obtained
261 from the literature (Krevelen & Nijenhuis, 2009; Liu et al., 2014a). These values, along with the physical
262 properties of the sample elements can be found in Table 1.

263

264 **2.6.1 Thermophysical and dielectric properties for the two-element model**

265 For the rice elements, temperature-dependent values of dielectric constant, loss factor, thermal
266 conductivity, specific heat, and density of were obtained from (Taguchi et al., 2025).

267 For the pore elements, the physical properties of air were used except for the thermal conductivity. The
268 reason for this was that it was necessary to account for the heat being transferred by water evaporating
269 at the hot spots, moving through the porous structure of the rice sample, and condensing in the cold spots.
270 Therefore, a value of apparent thermal conductivity was obtained using the same method as in our
271 previous study (Taguchi et al., 2025). This value was also used for the narrow space between the sample
272 and the PE lid, as it was considered that heat transfer could occur in a similar manner in this space.

273

274 **2.6.2 Thermophysical and dielectric properties of the apparent homogeneous sample**

275 The apparent homogeneous model was tested with three different values of the topology-related
276 parameter α , using the LK ($\alpha = 0$), CRIM ($\alpha = 0.5$), and LLL ($\alpha = 0.33$) mixture formulas (Eqs. 2-4).

277 These values have been used in several studies due to their proper theoretical basis, facilitating
278 comparison with the available literature while covering a somewhat wide range of topologies.

279 The value of penetration depth of microwaves at 2450 MHz was calculated according to the following
 280 relationship (Tanaka et al., 2005):

$$d_p = \frac{c}{2\pi f \sqrt{2\varepsilon' \left(\sqrt{1 + \left(\frac{\varepsilon''}{\varepsilon'}\right)^2} - 1 \right)}} \quad (18),$$

281 where c corresponds to the speed of light in vacuum (2.99×10^8 m/s). Penetration depth is defined as
 282 the distance at which the power decreases to $1/e$ of its initial value at the surface.

283 For the thermal conductivity, the method reported by Kunii & Smith (1960) was used. In this case, the
 284 apparent homogeneous sample was considered as a dispersion of void elements in a continuous phase of
 285 cooked rice. Therefore, the apparent thermal conductivity of the mixture k ($W/(m K)$) at different
 286 temperatures was obtained from the following relationship:

$$k = k_c \left[\phi - \frac{1 - \phi}{\eta + (2/3)(k_a/k_b)} \right] \quad (19),$$

287 where k_a and k_b are the thermal conductivity of rice and void elements respectively, as they were used
 288 in the two-element model (section 2.6.1), ϕ is the porosity (–), and η is an empirical constant obtained
 289 from the k_a/k_b relation (–). The values obtained at different temperatures were fit to a regression
 290 equation for each porosity.

291 The density ρ (kg/m^3) and specific heat C_p ($J/kg K$) of the apparent homogeneous sample were
 292 obtained from the volume fractions of rice V_a (–) and air V_b (–) within the sample using the following
 293 relations:

$$\rho = V_a \rho_a + V_b \rho_b \quad (20),$$

$$C_p = C_{pa} \rho_a + C_{pb} \rho_b \quad (21),$$

294 where ρ_a and C_{pa} are the density and specific of rice, and ρ_b and C_{pb} are the density and specific heat of
 295 air, obtained from (Taguchi et al., 2025).

296 The value or expression for all the thermophysical properties at 26 and 32 % porosity are shown in Table
297 1.

298

299 **2.7 Statistical analysis**

300 To test the differences between experimental and simulated results, the value of root mean square error
301 (RMSE) was obtained from the time-temperature data of N time steps during the MW heating treatments:

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N \left[\frac{T_{exp}(i) - T_{sim}(i)}{T_{exp}(i)} \right]^2} \quad (22),$$

302 where T_{exp} and T_{sim} are the experimental and simulated temperatures ($^{\circ}\text{C}$), respectively.

303

304 **3. RESULTS AND DISCUSSION**

305

306 **3.1 Topology of porous rice**

307 The X-ray CT images of the rice samples at 26 and 32 % are shown in Fig. 5. The values obtained for
308 the degree of anisotropy and porosity ratio are shown in Table 2. The results were considered sufficiently
309 accurate to serve as a confirmation of the porosity of the samples and the corresponding volumetric
310 fractions were used in the calculation of the thermophysical properties of the apparent homogeneous
311 sample.

312 A qualitative evaluation of the images shows highly interconnected pores in the samples, which ensure
313 gas, water, and heat exchange. No evidence of any ordered pattern or preferred orientation of the pores
314 was observed, which was further confirmed by the low degrees of anisotropy obtained for both samples
315 (Dhaliwal & Kumar, 2022). This is relevant because orientation of the lossy phase in the direction of the
316 electric field benefits charge movement, whereas discontinuity of the lossy phase in the direction of the

317 electric field causes a depolarization field which reduces the electrical flux density (Fujisaki, 2012). The
318 degree to which there is a preferred orientation of each of the phases defines the topology parameter α
319 that best describes the variation of dielectric properties with the volume fraction of the phases (Leao et
320 al., 2015; Nelson, 1992).

321 Additionally, the predictive model applied for MW heating in this study accounts for the heat transfer
322 due to vapor movement through the porous structure using a scalar value of apparent thermal conductivity.
323 Therefore, it assumes the isotropy of the vapor diffusivity such that the vapor has no preferable flow
324 direction within the sample (Warning et al., 2014).

325

326 **3.2 Dielectric properties of the samples**

327 Fig. 6 shows the dielectric properties, and the thermal conductivity of the samples as estimated from the
328 volume fractions obtained in 3.1. It can be seen that in the whole temperature range, CRIM estimated the
329 highest values of dielectric properties, followed by LLL and then by the LK model. This is the expected
330 results when decreasing values of α for a given sample (Regalado, 2004).

331 The calculated values of the dielectric properties decreased with increasing porosity, as more air
332 inclusions result in fewer polarizable molecules (Liu et al., 2009). The dielectric mixture equations
333 quickly account for this change by using a permittivity value of $\varepsilon = 1 + 0j$ for air. The penetration depth
334 of microwaves increased with porosity since it is inversely related to the dielectric loss factor.

335 It is worth noting that the estimated values differ more between mixture models than between porosities.
336 This is expected because each model assumes a different pore topology and the effect of the pore shape
337 on the permittivity has been found to be on the order of magnitude of the variation in permittivity due to
338 the porosity ratio (Jones & Friedman, 2000). This results in relatively low values of penetration depth
339 estimated by the CRIM equation: roughly around $2 - 3 \text{ cm}$. In contrast, LK equation estimated
340 penetration depths of approximately $3 - 4 \text{ cm}$.

341 The calculated thermal conductivity of rice decreased with porosity. This is consistent with the literature;
342 according to Ramesh (2000), thermal conductivity decreases with porosity in cooked rice due to
343 entrapped air which is a worse conductor than rice and water. In our case, an apparent value of thermal
344 conductivity was used for the pore fraction, but increasing its volume ratio still decreases the estimated
345 thermal conductivity of the mixture.

346

347 **3.3 MW heating behavior of cooked rice samples**

348 In the heating experiments, rice was placed in its original PP container, commonly used by consumers.
349 The low height of the container allows for fast and homogeneous heating in the flatbed MW oven used
350 in this study. This is because in this type of oven, microwaves enter from the bottom through the
351 waveguide, as seen in Fig. 7. If the container were taller, greater differences in electric field intensity
352 between the hot spots at the bottom and the cold spots at the top could be expected (Taguchi et al., 2025).
353 It is possible to appreciate the differences in electric field distribution between the two modeling
354 approaches. The two-phase model exhibits highly contrasting electric field intensities, even in contiguous
355 elements (Fig. 7a). In contrast, the electric field gradually distributes in discernible patterns within the
356 apparently homogeneous sample (Fig. 7b), as all its elements share the same dielectric properties.

357 The time-temperature histories of the rice samples during MW heating are shown in Fig. 8, with the
358 corresponding RMSE values listed in Table 3. A slightly faster heating of the 32 % porosity samples was
359 observed, especially from the edges. This is evidenced by the concave shape of the time-temperature
360 history curves in that position. In the 26 % porosity samples, the temperature at the edge was around
361 13 °C higher than that at the center by the end of the heating time. Whereas this difference was around
362 25 °C for the 32 % porosity samples.

363 This heating behavior is also evidence by the temperature distributions shown in Fig. 9. As early as $t =$
364 90 s, hot spots can be identified at the edges of the 32 % porosity sample, which are not observed in the

365 26 % sample. This is caused by its lower specific heat and thermal conductivity, which seems to have a
366 greater influence than its slightly higher penetration depth and lower loss factor. Similar results were
367 obtained by Yan et al. (2023) when studying the MW heating behavior of moderate-minced surimi with
368 different porosity ratios.

369 As expected, the two-element model gave good results for both porosities, as indicated by the consistently
370 low RMSE values. The small deviations from the experimental values can be attributed to the various
371 assumptions made in the simulation model. For example, water evaporation can affect the moisture
372 content and heating behavior of the samples, and this effect would also be affected by the porosity ratio
373 due to changes in the effective evaporation area (Li et al., 2019). Additionally, the thermal conductivity
374 of samples such as rice depends on its physical structure, especially of water binding to the starch
375 (Ramesh, 2000). The packed rice samples used in this study have already been thermally treated, but
376 some structural changes may still occur in the starch structure during reheating. Jiang et al. (2022) found
377 changes in the morphology of starch granules, in water binding capacity, and in the ordered structure of
378 starch chains after MW reheating of pregelatinized rice starch.

379 Finally, using calorimetric methods for the calculation of power absorption instead of more setting up
380 devices such as directional couplers can lead to deviations from the experimental conditions since the
381 energy absorption depends on the dielectric properties, geometry, and shape of the load (Kubo et al.,
382 2019; Liu et al., 2014a). The calorimetric methods, however, have been repeatedly validated in several
383 experimental settings; therefore, we consider the deviations originating from these assumptions to be
384 within an acceptable margin.

385

386 **3.4 Dielectric mixture equations**

387 Based on the RMSE values, no clear trend can be observed between the mixture models for the different
388 porosities, with values ranging from 0.06 to 0.35. However, as can be seen in the temperature

389 distributions (Fig. 9), the LK equation predicted heat accumulation towards the center of the container
390 regardless of the porosity ratio, suggesting an overestimation of the penetration depth. This did not result
391 in considerable deviations from the experimental time-temperature histories (Fig. 8) at 26 % porosity but
392 highly overestimated the final central temperature of the 32 % porosity sample resulting in a considerable
393 value of RMSE (0.30).

394 The intermediate penetration depth values calculated with the LLL equation predicted heat accumulation
395 in the center at 32 % porosity, but towards the edges at 26 % porosity. Similar to the LK equation, this
396 caused an abrupt jump towards the end of the time-temperature history curve at the center of the 32 %
397 porosity sample. The prediction for the 26 % porosity sample is in accordance with the experimental
398 values, albeit with a slight overestimation of the temperature difference between the edge and the center.
399 In the case of the CRIM equation, the low penetration depths predicted heat accumulation at the edges
400 of the sample regardless of the porosity ratio which is consistent with the experimental results and the
401 two-element model. The RMSE values were relatively stable but a slight overestimation of the heat
402 generation at the edges was observed.

403 For bread with 80 % porosity, Liu et al. (2009) found that the dielectric constant was predicted more
404 accurately by the LK equation but for the loss factor is was the LLL model the one which provided the
405 best estimations. Ozturk et al. (2018) found better results with the LK and the LLL equations on spices
406 with a volume fraction of around 0.40, and their mixtures. The CRIM equation showed better adequacy
407 to predict the dielectric properties of egg white powder with a volume ratio of 0.80 (Chen et al., 2019).

408 It is clear than the adequacy of one model over another depends more on how the dielectric properties
409 vary with volumetric fraction than on the volumetric fraction itself. Nelson (2005) reported a linear
410 dependency of the cube root of the permittivity of cereal grains and other granulated materials with bulk
411 density, which translated into more reliable estimates by the LLL equation. This linearity, in turn,

412 depends on the topology of the particles in the sample, and how it satisfies the assumptions under which
413 its specific α value was derived (Nelson, 1992).

414 Given the different heating patterns obtained for the mixture equations evaluated in this study, it could
415 be presumed that the value of α for the topology of the air pores in the cooked rice samples used in this
416 study lies somewhere outside of the three values applied in the present study, but closer to 0.5. This is
417 similar to the results obtained by (Leao et al., 2015) for average α values in soil samples. According to
418 the authors, these values suggest that the topology of the porous structure was close to isotropic. This is
419 consistent with the low degree of anisotropy obtained by X-ray CT analysis of the rice samples and
420 supports the apparent thermal conductivity approach applied in the MW heating simulations of the
421 present study.

422 Estimating accurate values or expressions for the α parameter using empirical methods that can better
423 represent the specific topology of the porous structure in different foods is desirable, since it allows for
424 dielectric mixture equations applicable to a wide range of porosity ratios. This gains significance given
425 that the two-element model approach is not feasible with many available finite-element software, and it
426 requires the size of the mesh elements to be comparable to that of the phases, which is not realistic when
427 the particle sizes are small, such as in emulsions or other dispersions.

428 In future studies, it may be desirable to compare the estimated and experimental values of dielectric
429 properties of rice and other multiphase food samples, to determine their specific α values. Additionally,
430 comparing the topological information of various porous foods with the permittivity-porosity
431 relationship could help correlate the α value with the degree of anisotropy and other topological data.

432

433 **4. CONCLUSIONS**

434 In this study, the dielectric properties of an apparent homogenous rice sample were estimated using
435 various dielectric mixture equations, their accuracy was assessed by comparing them with a two-element

436 MW heating model and experimental results, and the relationship between the adequacy of the models
437 and the topological structure of the sample was explored at two different porosities. The results of the X-
438 ray CT analysis confirmed the isotropic nature of the cooked rice samples. The evaluated mixture models
439 differed in their capacity to predict the heating behavior at the evaluated porosities. The CRIM equation
440 allowed for accurate predictions of the temperature distribution regardless of the porosity ratio, unlike
441 the LE and the LLL equations. Although the estimation of specific values of α that better reflect the
442 topology of the samples might be useful to obtain more accurate simulation models of dielectric heating
443 processes.

444

445 **Author statement**

446 Andres Abea: Data curation, formal analysis; investigation; methodology; writing – original draft.
447 Chihiro Sugihara: Formal analysis; investigation; methodology. Saki Sudou: Formal analysis;
448 investigation; methodology. Mark Anthony Redo: Methodology; writing – review and editing. Maria
449 Dolors Guàrdia: supervision; writing – review and editing. Israel Muñoz: supervision; writing – review
450 and editing. Yvan Llave: Conceptualization; supervision; writing – review and editing. Mika Fukuoka:
451 Conceptualization; methodology; resources; supervision; writing – review and editing.

452

453 **Declaration of competing interest**

454 The authors declare that they have no known competing financial interests or personal relationships that
455 could have appeared to influence the work reported in this paper.

456

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606

607 **Figure captions**

608 **Figure 1.** Bottom (a), top (b) and lateral view (c) of the polypropylene container three-dimensional model,
609 and longitudinal cut (d) for the inner temperature examination after the rice reheating experiments (all
610 sizes are in millimeters).

611 **Figure 2.** Position of the optic fiber sensors at the corner (a) and center (b) of the sample during the
612 heating experiments or rice on a flatbed MW oven (all sizes are in millimeters).

613 **Figure 3.** Schematic diagrams of the flatbed microwave oven and sample container used in this study.
614 View from the z-x (a) z-y (b) and x-y (c) directions (all sizes are in millimeters).

615 **Figure 4.** The two approaches used in the three-dimensional modeling of the rice samples.

616 **Figure 5.** X-ray computed tomography images of the rice samples with 26 % (a) and 32 (b) % porosity
617 for determination of porosity ratio and degree of anisotropy.

618 **Figure 6.** Calculated dielectric constant (a), dielectric loss factor (b), penetration depth (c) and apparent
619 thermal conductivity (d) of the apparent homogeneous sample model obtained with various mixture
620 equations at 26 and 32 % porosity from 20 to 90 °C.

621 **Figure 7.** Frontal cross-section of the electric field distribution (V/m) during MW reheating of cooked
622 rice on a flatbed microwave oven ($t=20$ s) simulated using a two-element (a) and apparent homogeneous
623 (b) model.

624 **Figure 8.** Experimental (mean values \pm standard deviation, $n=3$) and simulated temperatures as function
625 of MW heating time for: 26 % porosity rice at the edge (a), 26 % porosity rice at the center (b), 32 %
626 porosity rice at the edge (c), and 32 % porosity rice at the center (d) of the container.

627 **Figure 9.** Experimental temperature distribution of the longitudinal cross-section (Z-Y view) of 26 and
628 32 % porosity rice samples during heating on a flatbed MW oven and simulated results using different
629 approaches.

630

631

632 **Highlights**

- 633 - Microwave reheating simulations of an apparent homogeneous rice sample were built.
- 634 - Samples at two porosity values were modeled using dielectric mixture equations.
- 635 - Cooked rice samples at the evaluated porosity values had low degree of anisotropy.
- 636 - Different topologies assumed by each equation result in different heating patterns.
- 637 - The complex refractive index mixture equation shows slightly more accurate results.

638

639 **Table 1.** Physical properties of the materials used in the predictive simulation model of rice reheating
640 on a flatbed microwave model.

Parameter	Value or equation	Source
Dielectric constant ϵ' [-]		
Rice	$-0.0046T^2 + 0.3218T + 46.535$	Taguchi et al., 2024
Pores	1	Liu et al., 2014a
Air	1	Liu et al., 2014a
Apparent homogeneous sample 26 % (LK)	$-0.0013T^2 + 0.0901T + 17.151$	Present study
Apparent homogeneous sample 32 % (LK)	$-0.0009T^2 + 0.0655T + 13.641$	Present study
Apparent homogeneous sample 26 % (CRIM)	$-0.0027T^2 + 0.1933T + 27.942$	Present study
Apparent homogeneous sample 32 % (CRIM)	$-0.0023T^2 + 0.1659T + 24.395$	Present study
Apparent homogeneous sample 26 % (LLL)	$-0.0023T^2 + 0.1628T + 24.688$	Present study
Apparent homogeneous sample 32 % (LLL)	$-0.0019T^2 + 0.1339T + 20.963$	Present study
Loss factor ϵ'' [-]		
Rice	$0.0015T^2 - 0.2947T + 19.408$	Taguchi et al., 2024
Pores	0	Liu et al., 2014a
Air	0	Liu et al., 2014a
Apparent homogeneous sample 26 % (LK)	$0.0003T^2 - 0.0708T + 4.9123$	Present study
Apparent homogeneous sample 32 % (LK)	$0.0003T^2 - 0.0516T + 3.5642$	Present study
Apparent homogeneous sample 26 % (CRIM)	$0.0007T^2 - 0.1501T + 10.609$	Present study
Apparent homogeneous sample 32 % (CRIM)	$0.0006T^2 - 0.1289T + 9.1008$	Present study
Apparent homogeneous sample 26 % (LLL)	$0.0006T^2 - 0.1266T + 8.9245$	Present study
Apparent homogeneous sample 32 % (LLL)	$0.0005T^2 - 0.1043T + 7.3376$	Present study
Specific heat C_p [J/kg K]		
Rice	3080	Taguchi et al., 2024
Pores	1200	Liu et al., 2014a
Air	1200	Liu et al., 2014a
Apparent homogeneous sample 26 %	2478.54	Present study
Apparent homogeneous sample 32 %	2416.32	Present study
Density ρ [kg/m³]		
Rice	1060	Taguchi et al., 2024
Pores	1.2	Liu et al., 2014a
Air	1.2	Liu et al., 2014a
Apparent homogeneous sample 26 %	787.70	Present study
Apparent homogeneous sample 32 %	721.17	Present study
Thermal conductivity k [W/m K]		
Rice	0.319	Succar & Hayakawa, 1983
Pores	$0.025 \exp(0.116(T - 20))$	Taguchi et al., 2024
Air	0.025	Liu et al., 2014a
Apparent homogeneous sample 26 %	$0.023 \exp(0.067T)$	Present study
Apparent homogeneous sample 32 %	$0.035 \exp(0.056T)$	Present study

641 T : Temperature [°C]

642

643

644 **Table 2.** Values of porosity and degree of anisotropy of the two packed rice samples used in the
645 microwave heating experiments.

Sample	Porosity (%)	Degree of anisotropy (-)
26 %	26.34 ± 0.75	0.14 ± 0.01
32 %	32.49 ± 1.09	0.18 ± 0.02

646

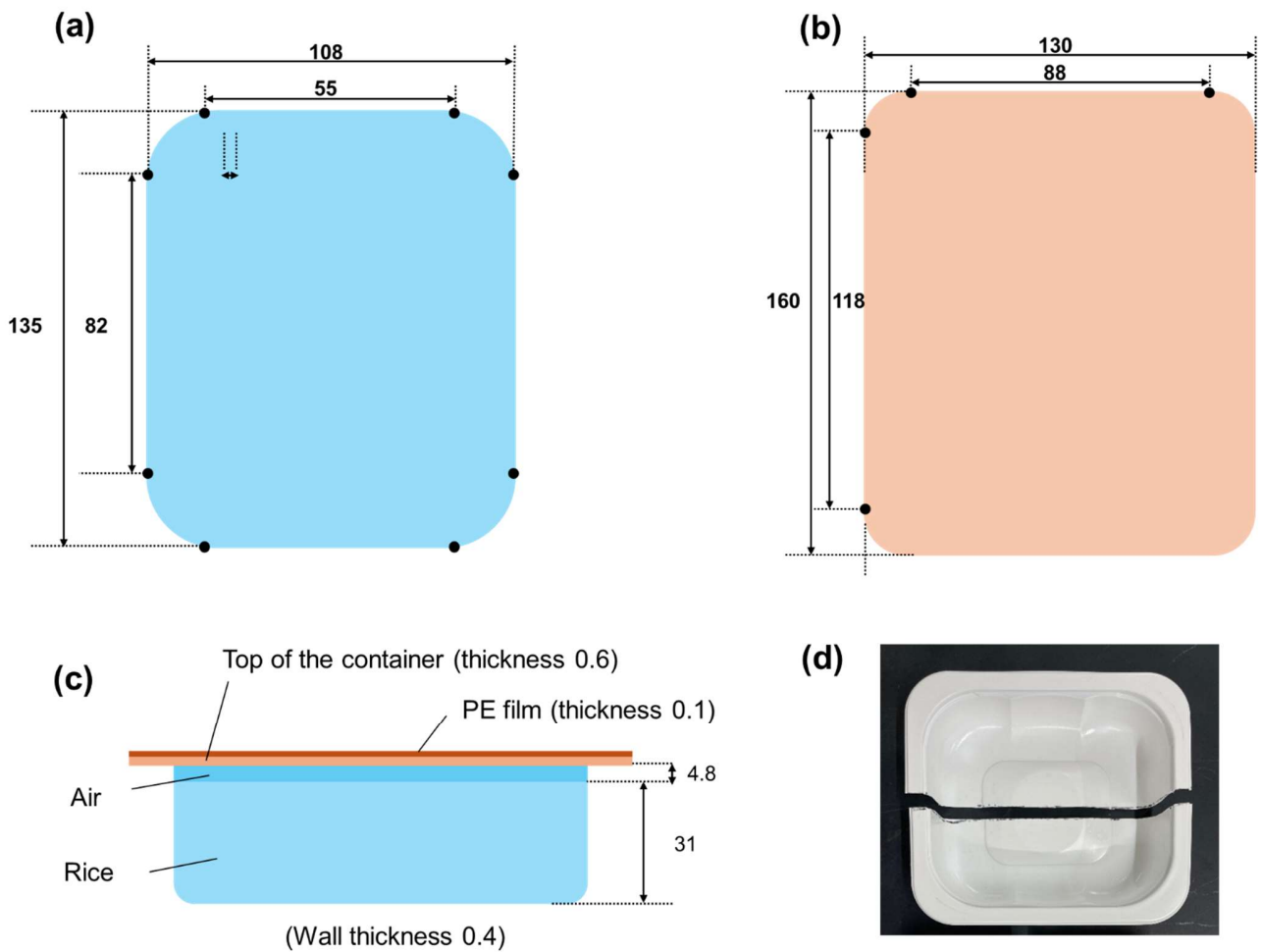
647

648 **Table 3.** Values of RMSE for the four approaches used in this study to simulate rice samples during
 649 heating on a flatbed microwave oven for 120 s.

Model	RMSE edge (-)	RMSE center (-)
Two-element model		
26 %	0.13	0.15
32 %	0.07	0.07
Apparent homogeneous model LK equation		
26 %	0.20	0.07
32 %	0.15	0.30
Apparent homogeneous model CRIM equation		
26 %	0.29	0.09
32 %	0.26	0.06
Apparent homogeneous model LLL equation		
26 %	0.35	0.13
32 %	0.18	0.18

650

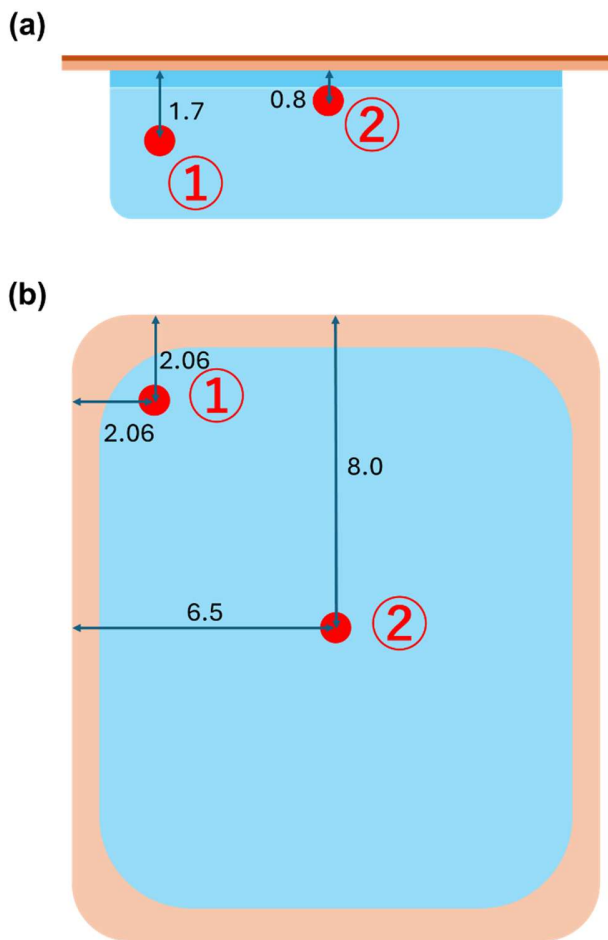
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652

653 **Figure 1.** Bottom (a), top (b) and lateral view (c) of the polypropylene container three-dimensional
 654 model, and longitudinal cut (d) for the inner temperature examination after the rice reheating
 655 experiments (all sizes are in millimeters).

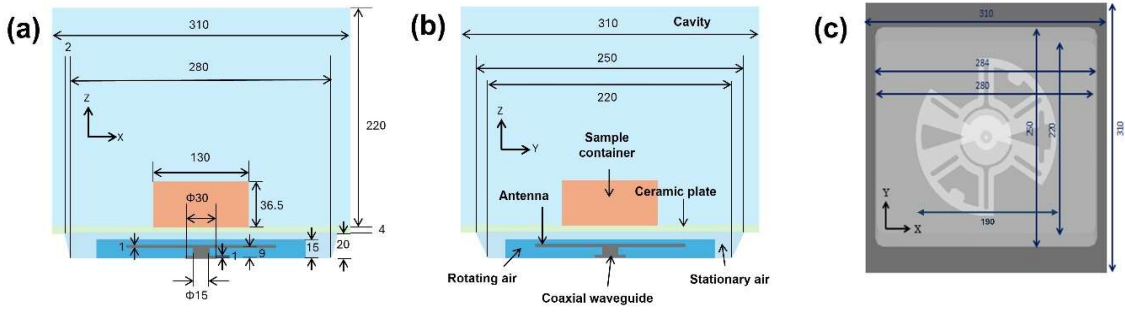
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657

658 **Figure 2.** Position of the optic fiber sensors at the corner (a) and center (b) of the sample during the

659 heating experiments of rice on a flatbed MW oven (all sizes are in millimeters).

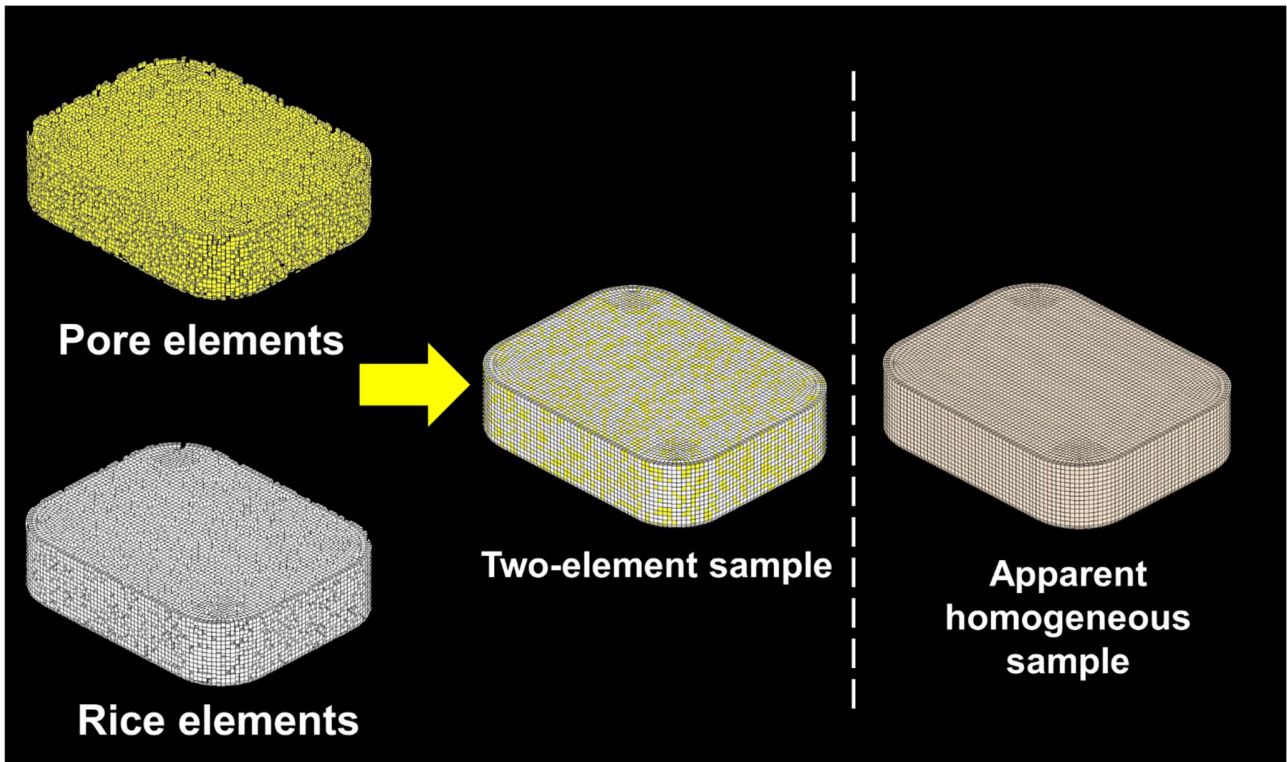


660

661 **Figure 3.** Schematic diagrams of the flatbed microwave oven and sample container used in this study.

662 View from the z-x (a) z-y (b) and x-y (c) directions (all sizes are in millimeters).

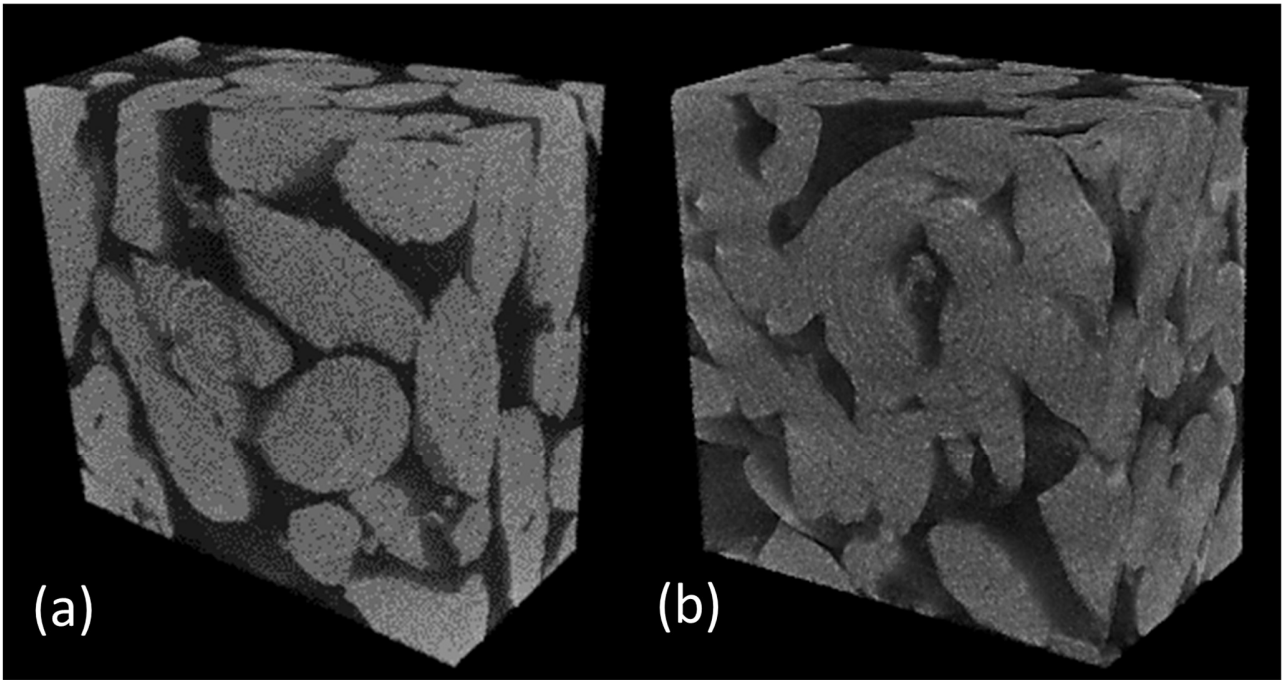
663



665

666 **Figure 4.** The two approaches used in the three-dimensional modeling of the rice samples.

667

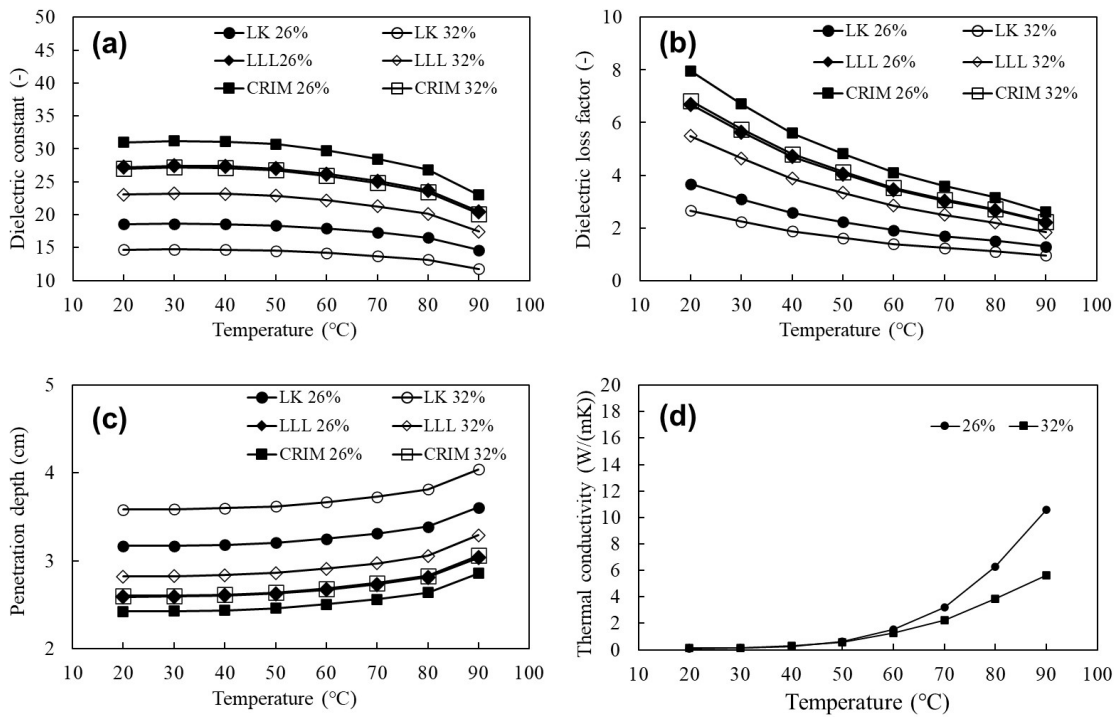


668

669 **Figure 5.** X-ray computed tomography images of the rice samples with 26 % (a) and 32 (b) % porosity

670 for determination of porosity ratio and degree of anisotropy.

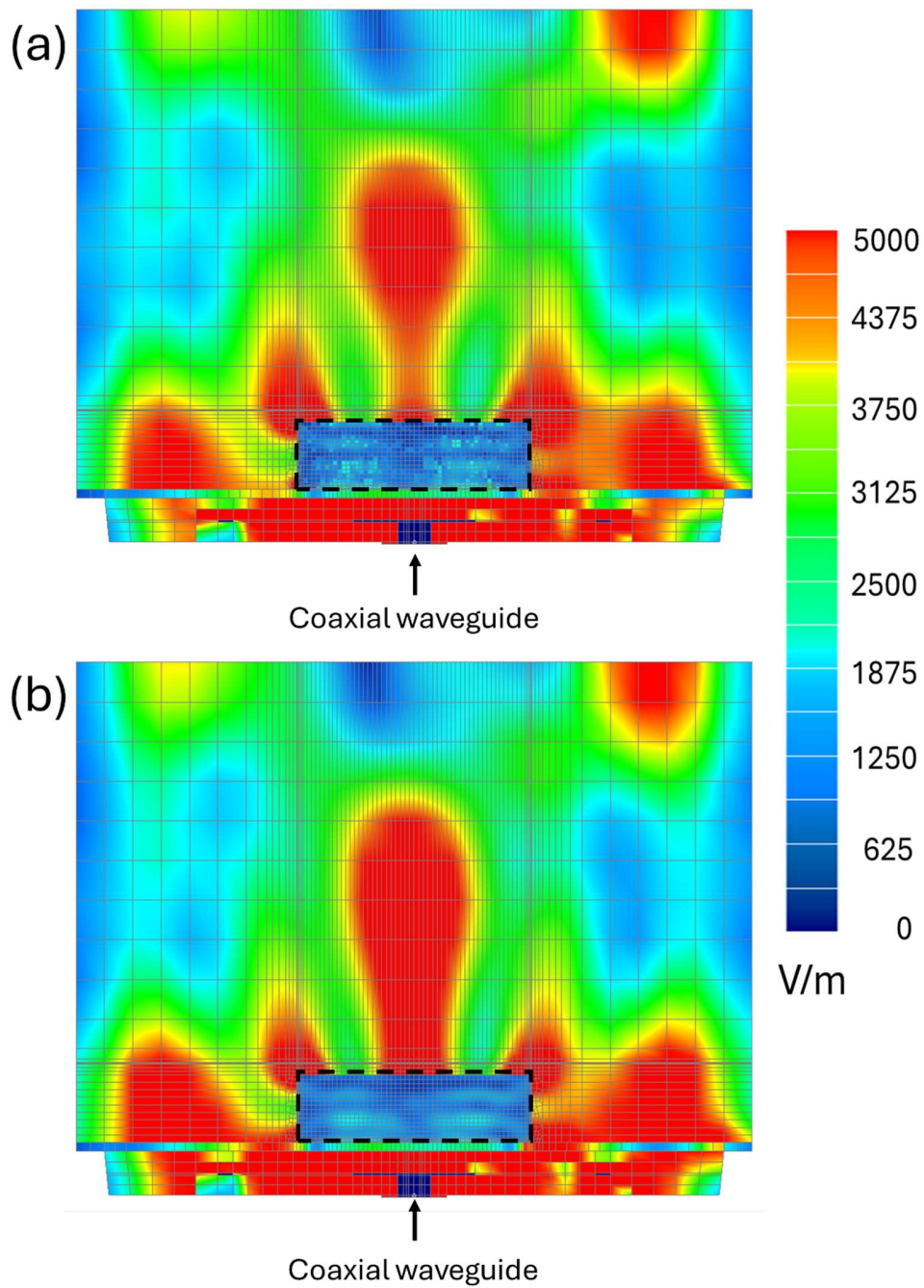
671



672

673 **Figure 6.** Calculated dielectric constant (a), dielectric loss factor (b), penetration depth (c) and apparent
 674 thermal conductivity (d) of the apparent homogeneous sample model obtained with various mixture
 675 equations at 26 and 32 % porosity from 20 to 90 °C.

676



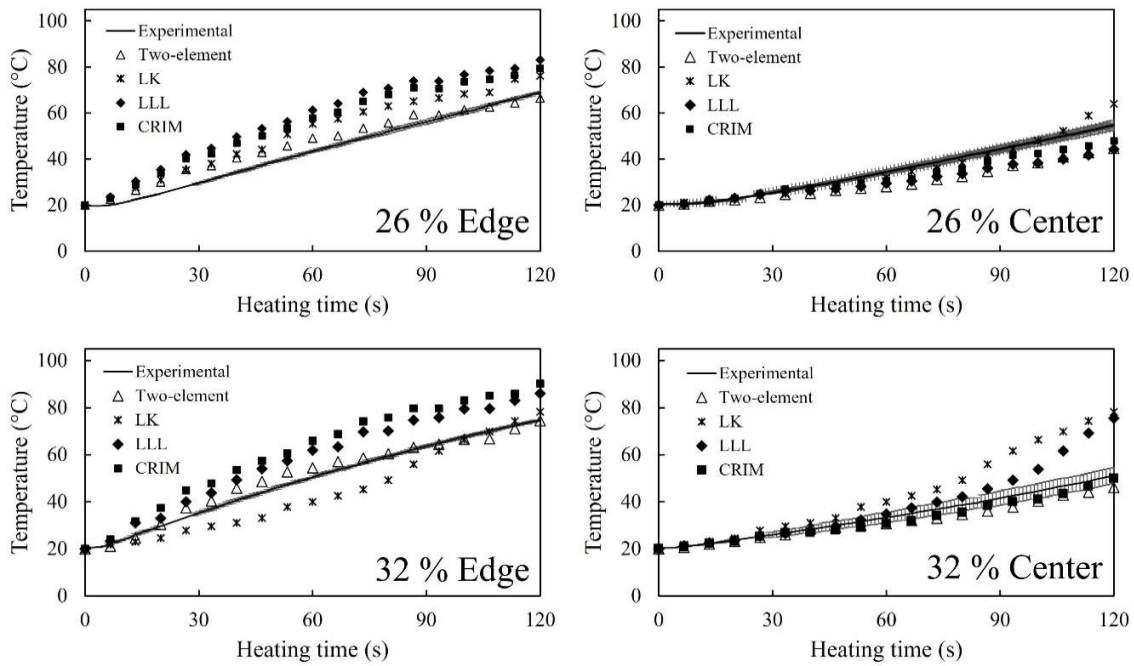
677

678 **Figure 7.** Frontal cross-section of the electric field distribution (V/m) during MW reheating of cooked

679 rice on a flatbed microwave oven ($t=20$ s) simulated using a two-element (a) and apparent

680 homogeneous (b) model.

681

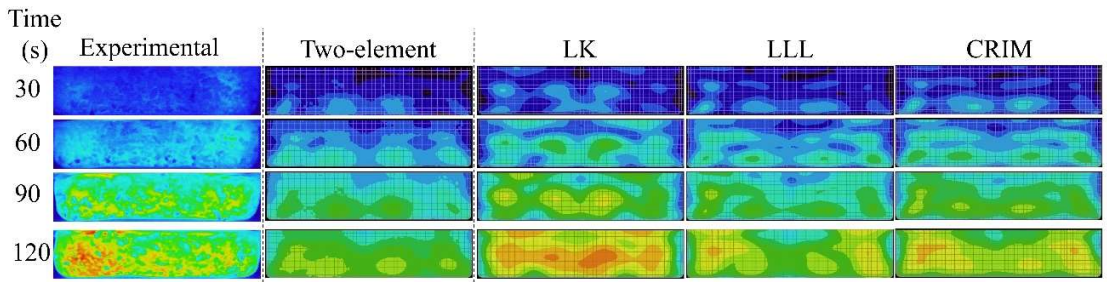


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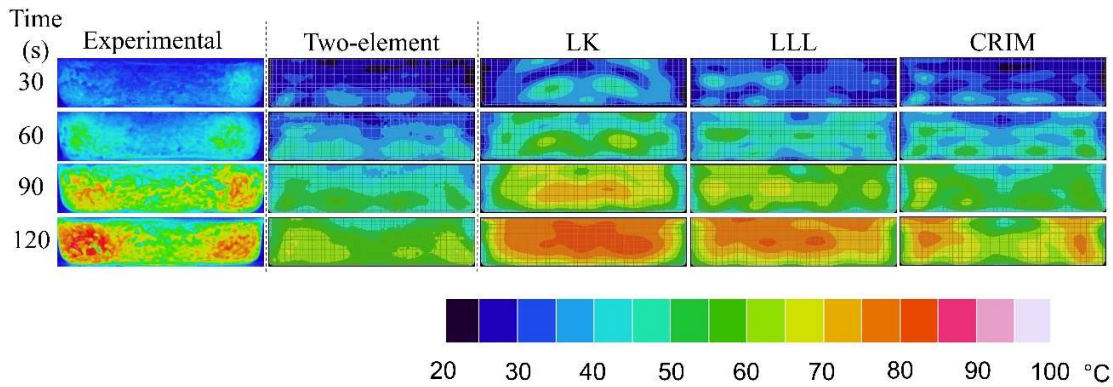
683 **Figure 8.** Experimental (mean values \pm standard deviation, $n=3$) and simulated temperatures as
 684 function of MW heating time for: 26 % porosity rice at the edge (a), 26 % porosity rice at the center
 685 (b), 32 % porosity rice at the edge (c), and 32 % porosity rice at the center (d) of the container.

686

26 %



32 %



687

688 **Figure 9.** Experimental temperature distribution of the longitudinal cross-section (Z-Y view) of 26 and
689 32 % porosity rice samples during heating on a flatbed MW oven and simulated results using different
690 approaches.

691

692 Figure S1.a shows the longitudinal cross-section (Z-Y view) of 26 and 32 % porosity rice samples
693 before the heating treatments. The volume remains unchanged between samples. The corresponding
694 amount for each porosity is placed inside the container gradually, while carefully mashing it until
695 reaching the fixed volume. It is worth noting that although there is only a difference of 6 % in porosity,
696 differences can be visually appreciated between the samples.

697

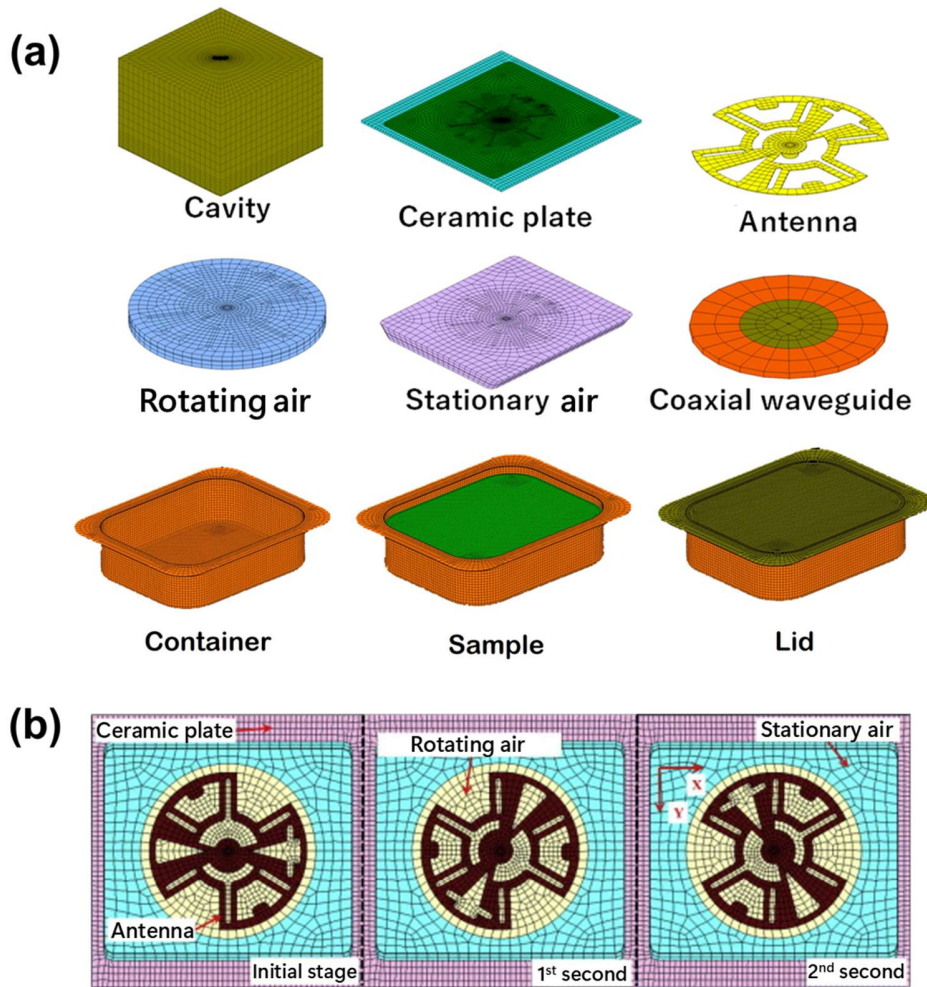


698

699 **Figure S1.** Longitudinal cross-section (Z-Y view) of 26 (a) and 32 % (b) porosity rice samples before
700 heating on a flatbed microwave oven.

701

702 Figure S2.a shows the mesh elements of the different domains in the flatbed microwave model. The
 703 equipment was dismantled, and the dimensions of the different components were measured. Figure
 704 S2.b illustrates the relation between the mesh of the stationary and rotating domains at the bottom of
 705 the cavity.



706
 707 **Figure S2.** Mesh of each domain in the 3D model of the flatbed microwave oven used in this study (a)
 708 and view direction of the stationary and rotating domains at the bottom of the cavity from the X-Y (b).